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Abstract: The IONORT-ISP system (IONOspheric Ray-Tracing - IRI-SIRMUP-PROFILES) was recently developed and tested by comparing the measured oblique ionograms over the radio link between Rome (41.89ºN, 12.48ºE), Italy, and Chania (35.51ºN, 24.02ºE), Greece, with the IONORT-ISP simulated oblique ionograms (Settimi et al., 2013). The present paper describes an upgrade of the system to include: a) electron-neutral collision have been included by using a collision frequency model that consists of a double exponential profile; b) the ISP three dimensional (3-D) model of electron density profile grid has been extended down to the altitude of the D-layer; c) the resolution in latitude and longitude of the ISP 3-D model of electron density profile grid has been increased from 2°x2° to 1°x1°. Based on these updates, a new software tool called IONORT-ISP-WC (WC means with collisions) was developed, and a database of 33 IONORT-ISP-WC synthesized oblique ionograms calculated for single (1-hop paths) and multiple (3-hop paths) ionospheric reflections. The IONORT-ISP-WC simulated oblique ionograms were compared with the IONORT-IRI-WC synthesized oblique ionograms, generated by applying IONORT in conjunction with the International Reference Ionosphere (IRI) 3-D electron density grid, and the observed oblique ionograms over the aforementioned radio link. The results obtained show that (1) during daytime, for the lower ionospheric layers, the traces of the synthesized ionograms are cut away at low frequencies because of HF absorption; (2) during night-time, for the higher ionospheric layers, the traces of the simulated ionograms at low frequencies are not cut off (very little HF absorption); (3) the IONORT-ISP-WC MUF values are more accurate than the IONORT-IRI-WC MUF values.

Dear Adv. Space Res. Past Editor in Chief, Dr. Peggy Ann Shea,
this cover letter is for re-submitting our manuscript (ASR-D-14-00169), entitled as:

“The IONORT-ISP-WC system: inclusion of an electron collision frequency model for the D-layer",

by the Authors,

Alessandro Settimi, Marco Pietrella, Michael Pezzopane, Cesidio Bianchi.

Please, let me know of your decision at your earliest convenience.

In attachments, You can find the word file of article, and the jpeg files of figures (dpi $\geq$ 600).

Moreover, we would like thanking the Reviewer 1 for his useful suggestions. We agree with him. We tried to change the paper in all the points that the Reviewer 1 has suggested. We have provided a detailed explanation in the attached reply letter.

Finally, in attachments, You can find a pdf file of the Reply to Reviewer 1.

With my best regards,
Sincerely yours,
Alessandro Settimi, PhD.

Second REVIEW OF:

Testing the IONORT-ISP system, with the inclusion of an electron collision frequency model for the D-layer

By

Alessandro Settimi, Marco Pietrella, Michael Pezzopane, Cesidio Bianchi

1. Recommendations

This paper has been re-worked enough that it can now be published, but with the indicated editorial changes.

I rewrote the abstract, on the grounds that this is the part of the paper that will be read by most readers.

2. General Comments

The convention is that the nose frequency on a real oblique ionogram is called the Maximum Observed Frequency (MOF). The term MUF could mean the instantaneous predicted value of the nose frequency (as in this paper) or the median nose frequency for a set of HF propagation predictions.

I still maintain that if you are going to compare calculated MUFs with MOFs from a physical system, you have to discuss SNR and antenna gains. But perhaps that would be the next step.

This paper deserves a mention: "McNamara, L. F., M. J. Angling, S. Elvidge, S. V. Fridman, M. A. Hausman, L. J. Nickisch, and L.-A. McKinnell (2013), *Assimilation procedures for updating ionospheric profiles below the F2 peak*, Radio Sci., 48, doi:10.1002/rds.20020." The comparisons of the 1F MUFs and MOFs were based on Jones-type raytracing, but the authors considered this to be just another tool in their toolbox.

Authors: OK. We agree with the Reviewer 1. The revised manuscript was updated mentioning in the reference section the Mc Namara et al. (2013) article.

3. Suggested Revised Abstract

The IONORT-ISP system (IONOspheric Ray-Tracing – IRI-SIRMUP-PROFILES) that was recently developed and tested by comparing the measured oblique ionograms over the radio link between Rome (41.89ºN, 12.48ºE), Italy, and Chania (35.51ºN, 24.02ºE), Greece, with the IONORT-ISP simulated oblique ionograms [reference]. The present paper describes an upgrade of the system to include : a) electron -neutral collisions have been included by using a collision frequency model that consists of a double exponential profile; b) the ISP three dimensional (3-D) model of electron density profile grid has been extended down to the altitude of the D-layer; c) the resolution in latitude and longitude of the ISP 3-D model of electron density profile grid has been increased from 2◦x2◦ to 1◦x1◦. Based on these updates, a new software tool called IONORT-ISP-WC (WC means with collisions) was developed, and a database of IONORT-ISP-WC synthesized oblique ionograms calculated for single (1-hop paths) and multiple (3-hop paths) ionospheric reflections was produced. The IONORT-ISP-WC simulated oblique ionograms were compared with the IONORT-IRI-WC synthesized oblique ionograms, generated by applying

IONORT in conjunction with the International Reference Ionosphere (IRI) 3-D electron density grid, and the observed oblique ionograms over the Rome to Chania path. The results obtained show that (1) during daytime, for the lower ionospheric layers, the traces of the synthesized ionograms are cut away at low frequencies because of HF absorption; (2) during night-time, for the higher ionospheric layers, the traces of the simulated ionograms at low frequencies are not cut off (very little HF absorption); (3) the IONORT-ISP-WC MUF values are more accurate than the IONORT-IRI-WC MUF values.

Authors: OK. We agree with the Reviewer 1. The revised manuscript was updated rewriting the abstract, and including the reference, as suggested.

4. Small Revisions

Small font size indicates that this text is to be removed.

2/36 management of HF radio communications, and the predictions of the operating frequencies, are

2/56 of the wave along the path, and other optional quantities such as absorption, polarization, etc. The

2/61 Croft and Gregory, 1963; Jones, 1966) ran on old mainframes that provided only a numerical output. *They were not "old" – they were very modern.*

3/2 Cannon (1997) developed a two dimensional (2-D) analytic ray-tracing method called SMART for

3/10 ray-trace through complicated horizontal gradients along and in the direction of the ray path.

3/17 for a real-time use.

3/19 Recently an applicative software tool package named IONORT (IONOspheric Ray-Tracing), able to

3/20 work both with analytical and numerical electron density models, was developed at the Istituto

3/24,26 HF waves propagating in the

3/29 The validity of IONORT

4/0 the INGV, the IRI-SIRMUP-PROFILES (ISP) model, capable of providing a 3-D electron density

4/2 profile representation of the ionosphere in quasi real time, was developed.

4/17 Recently IONORT was used in conjunction with two kinds of 3-D electron density grids: one

4/39 shown that the ISP model can more accurately represent real conditions in the ionosphere than the

4/48 between electrons and neutral particles, consisting of a double exponential profile (Jones and

4/53 were made; the ISP electron density profile grid is also modified starting now with the D-layer

5/5 examples of the IONORT-ISP-WC synthesized oblique ionograms are shown and discussed in terms

5/12 the IONORT-ISP system. We describe our results in Section 3.
5/41 There is a large number of electron collision frequency models, for example constant collision
5/42 frequency, and exponential and tabular profiles (see references therein Jones and Stephenson,
6/2 electrons and neutrals for the D-layer that consists of a double exponential profile (Jones and
6/15 Would you care to explain the physics behind the two separate slopes?
6/47 COMPLEIK is just as reliable as ICEPAC, with the advantage of being implemented more GREEN highlighting?? YUK!
6/51 profiles corresponding to the COMPLEIK are just as reliable as the ICEPAC formula, for
7/0 In order to plot the ionogram with and without absorption, each Each synthesized ionogram was
7/22 by a typical absorption coefficient, i.e. $L \leq$ 20 dB, but does not show the trace of E-layer with a
7/32 This section discusses some examples of the ray path calculated by means of the proposed IONORTISP-WC system, and some results obtained by comparing the IONORT-ISP-WC synthesized oblique ionograms with the IONORT-IRI-WC synthesized oblique ionograms and the oblique ionograms measured along the Rome-Chania radio link are also discussed.
7/56 were either noisy or characterized by interference phenomena preventing users from accurately
8/24 ISP model (-10° – 40° in longitude, 30° – 50° in latitude). The ray paths were calculated taking into
8/56 Fig. 3 shows an example of an oblique ionogram recorded over the Rome-Chania radio link on 07 July
9/5 The case of Fig. 3 shows clearly that the inclusion of the electron collision frequency model for the
9/10 low frequencies for the lower ionospheric layer (E region). As expected, both for 1-hop paths and 3-
9/36 MHz in case of WC; in this case a trace 6.8 MHz long is missing because of absorption suffered by
9/46 It must be noted that the MUF values calculated with or without the collisions model, in all the
9/48 cases analyzed show always the same value when a given electron density model is applied (IRI or
10/5-7 comprehensive comparison, no-collision (NC) cases are also included the cases obtained without applying the collisional model of Eq. 1 which are indicated with NC.
10/12 when the absorption of the propagating wave through the ionosphere can be considered negligible
10/29 practically occurs for the epoch 26 June 2011 at 01:00 UT where only very small differences are
10/56 and the measured MUF values. From the results shown in the columns D and E, it can be seen that
11/14 Fig. 5 the green squares marked with the symbol *) is the performance of IONORT-IRI-WC is better

10/29 on the whole database, it emerges that the IONORT-ISP-WC MUF values are more accurate than the
10/51 Gibilmanna, and the only reference ionospheric station contributing to the ISP grids was Athens.
12/14 IONORT-ISP-WC system in providing consistent results.

Authors: OK. We agree with the Reviewer 1. The revised manuscript was updated including all these small revisions throughout the text body.

The IONORT-ISP-WC system: inclusion of an electron collision frequency model for the D-layer

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Abstract

The IONORT-ISP system (IONOspheric Ray-Tracing – IRI-SIRMUP-PROFILES) was recently developed and tested by comparing the measured oblique ionograms over the radio link between Rome (41.89ºN, 12.48ºE), Italy, and Chania (35.51ºN, 24.02ºE), Greece, with the IONORT-ISP simulated oblique ionograms (Settimi et al., 2013). The present paper describes an upgrade of the system to include: a) electron-neutral collision have been included by using a collision frequency model that consists of a double exponential profile; b) the ISP three dimensional (3-D) model of electron density profile grid has been extended down to the altitude of the D-layer; c) the resolution in latitude and longitude of the ISP 3-D model of electron density profile grid has been increased from 2°x2° to 1°x1°. Based on these updates, a new software tool called IONORT-ISP-WC (WC means with collisions) was developed, and a database of 33 IONORT-ISP-WC synthesized oblique ionograms calculated for single (1-hop paths) and multiple (3-hop paths)

ionospheric reflections. The IONORT-ISP-WC simulated oblique ionograms were compared with the IONORT-IRI-WC synthesized oblique ionograms, generated by applying IONORT in conjunction with the International Reference Ionosphere (IRI) 3-D electron density grid, and the observed oblique ionograms over the aforementioned radio link. The results obtained show that (1) during daytime, for the lower ionospheric layers, the traces of the synthesized ionograms are cut away at low frequencies because of HF absorption; (2) during night-time, for the higher ionospheric layers, the traces of the simulated ionograms at low frequencies are not cut off (very little HF absorption); (3) the IONORT-ISP-WC MUF values are more accurate than the IONORT-IRI-WC MUF values.

Keywords: Ray-Tracing; Electron Density; IRI; Assimilative Modelling; Oblique Ionogram; Electron collision frequency model.

1. Introduction

Ionospheric ray-tracing is a technique used to determine the path of a high frequency (HF) radio wave propagating in the ionosphere from a transmitting point to a receiving point.

Over the horizon radar systems, single station location, HF direction finding systems, the management of HF radio communications, and the predictions of operating frequencies, are examples of the main applications of ray-tracing, where a detailed knowledge of radio wave propagation through the ionosphere is needed.

Accurate ray-tracing is usually performed using numerical techniques requiring Haselgrove's equations (Haselgrove, 1955; Haselgrove and Haselgrove, 1960). The propagation of the wave, i.e., the ray path, is described by six differential equations where the parameters of both the position and ray direction need to be integrated simultaneously at each point along the ray path. The integration provides the coordinates reached by the wave vector and its three components, the group time delay of the wave along the path, and other optional quantities such as absorption, polarization, etc. The

first ray-tracing algorithms developed in the 1960s (Dudziak, 1961; Lawrence and Posakony, 1961; Croft and Gregory, 1963; Jones, 1966) ran on old mainframes that provided only a numerical output. Since then, many other ray-tracing programs have been developed. For example, Norman and Cannon (1997) developed a two dimensional (2-D) analytic ray-tracing method called SMART for which computer run times are about 10 times faster than those of numerical ray-tracing packages. SMART automatically segments the ionosphere in terms of ground range and it is able to accurately ray-trace through complicated horizontal gradients along the direction of the ray path. Nowadays, the modern ray-tracing procedures (Coleman, 1998; Nickisch, 2008) have been optimized and adapted to over the horizon radar applications using powerful computers and devices for real-time use.

Recently an applicative software tool package named IONORT (IONOspheric Ray-Tracing), able to work both with analytical and numerical electron density models, was developed at the Istituto Nazionale di Geofisica e Vulcanologia (INGV), for calculating a 3-D ray-trace for HF waves propagating in the ionospheric medium (Azzarone et al., 2012).

The validity of IONORT was checked by comparing at different frequencies the time delay of the wave that results from the ray-tracing computation performed by IONORT (t_{calc}), and the time delay of the wave propagating along the oblique virtual path at the speed of light (t_{virt}). It was found that the IONORT ray-tracing algorithm fits nearly perfectly the theory so that the relative error $\Delta t = t_{calc} - t_{virt}$ is only due to the discrete integration step (Bianchi et al., 2011).

Ray-tracing can generally be performed accurately if the 3-D electron density distribution between the transmitter and the receiver is known (Kashcheyev et al., 2012). A comprehensive specification of the ionosphere in terms of electron density, neutral particles – electrons collision frequency, and geomagnetic field is required in order to carry out an accurate ray-tracing. Therefore, when dealing with near real-time applications of ray-tracing, it is of crucial importance to have a realistic ionospheric modelling through 3-D models of ionospheric electron density, which after assimilating measured data calculate an updated 3-D image of the ionosphere (Angling and Khattatov, 2006;

Thompson et al., 2006; Fridman et al., 2006, 2009; Decker and McNamara, 2007; McNamara et al., 2007, 2008, 2010, 2011, 2013; Angling and Jackson-Booth, 2011; Shim et al., 2011). More recently, at the INGV, the IRI-SIRMUP-PROFILES (ISP) model, capable of providing a 3-D electron density profile representation of the ionosphere in quasi real time, was developed.

The ISP model has proven very effective in providing reliable electron density profiles under quiet and disturbed geomagnetic conditions in several studies (Pezzopane et al., 2011, 2013). In particular at the solar terminator, the electron densities calculated by the ISP model more accurately represented the real conditions of the ionosphere than electron densities calculated using the climatological IRI-URSI model alone.

Recently IONORT was used in conjunction with two kinds of 3-D electron density grids: one generated by the International Reference Ionosphere (IRI) electron density model; and the other one outputted by the ISP model (Pezzopane et al., 2011) after assimilating autoscaled foF2 and M(3000)F2 data, and real-time vertical electron density profiles from the reference stations of Rome (41.8ºN, 12.5ºE), Gibilmanna (37.9ºN, 14.0ºE) in Italy, and Athens (38.0ºN, 23.5ºE) in Greece.

Synthesized oblique ionograms over the radio link between Rome and Chania (35.51ºN, 24.02ºE), Greece, were produced by the IONORT-IRI and IONORT-ISP system and compared with the measured oblique ionograms (Settimi et al., 2013). The comparisons carried out both in terms of the ionogram shape and the maximum usable frequency (MUF) characterizing the radio path have shown that the ISP model can more accurately represent real conditions in the ionosphere than the IRI model, and that the ray-tracing results computed by IONORT are reasonably reliable.

The present paper is inspired by the abovementioned Settimi et al. (2013) study. With the aim of extending this study, the IONORT-ISP system was upgraded including a collision frequency model between electrons and neutral particles, consisting of a double exponential profile (Jones and Stephenson, 1975). Moreover, some changes with respect to the previous version of the ISP model were made; the ISP electron density profile grid is also modified starting now with the D-layer (starting point at 65 km) and increasing the resolution in latitude and longitude from 2°x2° to 1°x1°.

On the basis of these updates, a new software tool package, to which we refer hereafter as IONORT-ISP-WC (WC, means with collisions), was developed and a database of 33 IONORT-ISP-WC synthesized oblique ionograms completed with single (1-hop paths) and multiple (3-hop paths) ionospheric reflections was produced over the same radio link aforementioned. Some representative examples of the IONORT-ISP-WC synthesized oblique ionograms are shown and discussed in terms of comparison with the IONORT-IRI-WC synthesized oblique ionograms and the observed oblique ionograms. Section 2 describes the electron collision frequency model for the D-layer included in the IONORT-ISP system. We describe our results in Section 3. Concluding remarks and possible future developments are summarized in section 4.

2. Description of the electron collision frequency model for the D-layer

Collisions of free electrons with neutrals, heavy ions, or other electrons are important causes of various macroscopic phenomena. Electron collisions play an important role in the absorption of radio waves at lower altitudes (D-layer) (Settimi et al., 2014). Using an appropriate theory (Davies, 1990) it is possible to deduce the electron collision frequency from radio wave propagation data. According to Budden (1965), for a detailed quantitative interpretation of some experiments it is necessary to apply the generalized theory (Sen and Wyller, 1960), while for most practical radio propagation problems, the classical theory (Appleton and Chapman, 1932) is adequate, especially when appropriate values are available for the effective electron collision frequency.

There is a large number of electron collision frequency models, for example constant collision frequency, and exponential and tabular profiles (see references in Jones and Stephenson, 1975**)**. It should be noted that if users want to implement other collision frequency models, they must write a subroutine to calculate the normalized frequency $Z=\nu/2\pi f$ (where ν is the collision frequency between electrons and neutral air molecules, and f is the transmitted wave frequency) and its gradients ($\partial Z/\partial r$, $\partial Z/\partial \theta$, $\partial Z/\partial \varphi$) as a function of position within spherical polar coordinates (r, θ, φ)

referring to a system of computational coordinates (which is not necessarily the same as geographic coordinates).

The current version of the IONORT-ISP-WC system includes a collision frequency model between electrons and neutrals for the D-layer that consists of a double exponential profile (Jones and Stephenson, 1975)

$$\nu(h) = \nu_1 e^{-a_1(h-h_1)} + \nu_2 e^{-a_2(h-h_2)}, \quad (1)$$

where v is the collision frequency at the height above ground h. The first exponential has the following specifications: collision frequency at height h_1, $\nu_1=3.65\cdot10^4$ collisions per second; reference height, $h_1=100$ km; exponential decrease of v with height, $a_1=0.148$ km^{-1}. The second exponential has the following specifications: collision frequency at height h_2, $\nu_2=30$ collisions per second; reference height, $h_2=140$ km; exponential decrease of v with height, $a_2=0.0183$ km^{-1}. Fig. 1 shows the trend of the electron collision frequency implemented in the IONORT-ISP-WC system.

It should be noted that, in Settimi et al. (2014) paper, simple complex eikonal equations, in quasi-longitudinal (QL) approximation (Rawer, 1976), for calculating the non-deviative absorption coefficient due to the propagation across the D-layer were encoded into a so called COMPLEIK (COMPLex EIKonal) subroutine of the IONORT program. The IONORT program already included the same electron collision frequency model for the D-layer, consisting of the double exponential profile (Jones and Stephenson, 1975). As main outcome of that paper, the simple COMPLEIK algorithm was compared to the more elaborate semi-empirical ICEPAC formula (Stewart, undated). COMPLEIK is just as reliable as ICEPAC, with the advantage of being implemented more directly. Settimi et al. (2014), applying just Eq. 1 (Fig. 1), proved that, the non-deviative absorption profiles corresponding to COMPLEIK are just as reliable as the ICEPAC formula, for all the ordinary and extraordinary rays effectively radio linking Rome and Chania. Instead, the absorption profiles

corresponding to the COMPLEIK subroutine lose their reliability just for all the rays that cannot establish the radio link Rome-Chania.

Each synthesized ionogram was computed with or without applying the electron collision frequency model. For the sake of clarity, the synthesized ionograms are generated considering only the ordinary trace and taking into account the geomagnetic field.

For all cases, with the exclusion of those at the solar terminator and during the night, an oblique ionogram computed without applying the electron collision frequency model (1) consists of (e.g., Settimi et al., 2014): 1) a trace for the ionospheric F1-F2 layers at high altitudes (h>150 km); 2) a trace for the E-layer at lower altitude (90 km<h≤150 km). Generally, an ionogram computed applying the electron collision frequency model (1) shows the trace of F1-F2 layers, characterized by a typical absorption coefficient, i.e. L≤20 dB, but does not show the trace of E-layer with a higher absorption coefficient, i.e. L>>20 dB (e.g., McNamara, 1991).

3. Results and Discussion

This section discusses some examples of the ray path calculated by means of the proposed IONORT-ISP-WC system and some results obtained by comparing the IONORT-ISP-WC synthesized oblique ionograms with the IONORT-IRI-WC synthesized oblique ionograms and the oblique ionograms measured along the Rome-Chania radio link. The database of the observed oblique ionograms used in this study, is constituted by 33 oblique ionograms recorded over the Rome-Chania radio link in June, July, and October 2011 in the daytime, night-time, at sunrise, and at sunset during quiet and moderate geomagnetic activity.

The ionograms comprising this database were selected on the criteria of: a) clarity of trace, which is essential in order to perform a trace shape comparison between measured and synthesized ionograms. In this respect it is worth noting that often the recorded Rome-Chania radio link traces were either noisy or characterized by interference phenomena preventing users from accurately validating the MUF, in addition to not being tagged for polarization; b) most of the ionograms had

to be recorded at specific times for which both the Athens autoscaling, and at least one between the Rome and Gibilmanna autoscalings were available and essentially correct. These "boundary conditions" greatly limited the number of measured oblique ionograms in the test database. The b) requirement is necessary to guarantee that the assimilation process was properly performed with data from at least two ionospheric stations located close to the two extremities of the radio path. It will be seen in Section 4 that the assimilation of data from only one station at only one extremity of the radio path can cause significant underestimation/overestimation of the real MUF.

Fig. 2 shows four examples of the IONORT's graphical user interface (for a more detailed description of this interface, see Azzarone et al., 2012).

Each example shows the 2-D (at the bottom) and 3-D (on the right side) ray paths along the Rome-Chania radio link (azimuth angle equal to 121.6°), which falls beyond the validity area of regional ISP model (-10° – 40° in longitude, 30° – 50° in latitude). The ray paths were calculated taking into account the geomagnetic field, the electron collision frequency model for the D-layer (Eq. 1), and the electron density profile grid calculated at the epoch 26 June 2011 at 01:00 UT by the global IRI model.

It must be noted that the IONORT-IRI-WC system, with respect to the previous version IONORT-IRI, is now able to provide ray paths also with multiple (3-hop paths) ionospheric reflections, as shown for the two cases depicted at the bottom of Fig. 2.

In all the synthesized ionograms with single or multiple ionospheric reflections (1 – 3 hop paths), even though the ionosphere is not characterized by large horizontal gradients, a nested loop cycle was iterated with azimuth angles from 121° to 122° of step 0.2°. The elevation angle step was set to 0.2° and the receiver (RX) range accuracy to 0.1 % (for a more detailed description of how the parameters, i.e. azimuth, elevation steps and RX range accuracy, are used in the ray-tracing program, we refer the reader to Appendix A of Settimi et al., 2013).

Fig. 3 shows an example of an oblique ionogram recorded over the Rome-Chania radio link on 07 July 2011 at 15:00 UT (top panel), and its corresponding synthesized ionograms generated by the

IONORT-IRI-WC (middle panel) and IONORT-ISP-WC (bottom panel) system. The cases labelled with NC (NC means No Collisions) obtained without including the electron collision frequency model for the D-layer (Eq. 1) are also shown for a further and more comprehensive comparison.

The case of Fig. 3 shows clearly that the inclusion of the electron collision frequency for the D-layer during daytime has the effect of cutting away the trace of the synthesized ionogram at the low frequencies for the lower ionospheric layer (E region). As expected, both for 1-hop paths and 3-hop paths, the Lowest Observed Frequencies (LOF) calculated not taking into account the collisional model, both in case of IRI and ISP electron density profile grids, are systematically much smaller than those calculated when the collisional model provided by the Eq. 1 is applied. More precisely looking at 1-hop paths, for IRI electron density profile grids (see second panel of Fig. 3), LOF_E = 4.2 MHz with NC and LOF_E = 10.0 MHz in case of WC, so that a trace long 5.8 MHz is cut off because of absorption; for the higher ionospheric layer (F region) LOF_F = 5.6 MHz with NC and LOF_F = 5.5 MHz in case of WC, which means that the trace is not cut off. This is also an expected result because at the height of F region the effect of the collisions is less important and therefore the waves propagating at a given frequency do not suffer an important absorption. For ISP electron density profile grids (see third panel of Fig. 3), LOF_E = 3.1 MHz with NC and LOF_E = 9.9 MHz in case of WC; in this case a trace 6.8 MHz long is missing because of absorption suffered by the wave propagating at the height of E region. Again, at higher heights the effect of the collisions on the propagating waves can be considered negligible because the calculated LOF values are similar being LOF_F = 9.0 MHz with NC and LOF_F = 8.8 MHz in case of WC.

It must be noted that the MUF values calculated with or without the collisions, in all the cases analyzed show the same value when a given electron density model is applied (IRI or ISP); this is a reasonable result because MUF depends only on the highest frequency reflected by the F2-layer, (foF2), and the secant of the optimum angle at which to broadcast a signal that is to be received at a given distance *D*, (M(*D*)F2).

The two cases in Fig. 4 show an example of oblique ionograms recorded over the Rome-Chania radio link on 9 October 2011 at 03:00 UT (at the top, on the left), and 26 June 2011 at 01:00 UT (at the top, on the right) with their corresponding synthesized ionograms generated by the IONORT-IRI-WC (middle panels) and IONORT-ISP-WC (bottom panels). For a further and more comprehensive comparison, no-collision (NC) cases are also included.

It should be noted that these two examples are relative to ionograms observed during night-time when the absorption of the propagating wave through the ionosphere can be considered negligible because of the lack of the lower absorbing layers (D and E regions). For this reason, the LOF_F calculated with or without the electron collision frequency model for the D-layer show practically the same values. To better clarify this feature, we can refer to the legends of Fig. 4 where the LOF_F values are reported. For the epoch 9 October 2011 at 03:00 UT, both for IRI and ISP electron density profile grids (see second and third panel of Fig. 4 respectively), the LOF_F values calculated with or without the collisional model are equal to 3.0 MHz for 1-hop and 3-hop paths. The same occurs for the epoch 26 June 2011 at 01:00 UT where only very small differences are observed between the LOF_F calculated with NC and the LOF_F obtained in the case WC: discrepancies of 0.1 MHz (for 3-hop paths) and 0.4 MHz (for 1-hop paths) are observed when the IRI and ISP electron density profile grids are considered respectively, which means that during night-time the simulated ionograms do not show traces cut away at lower frequencies.

The results of this study are summarized in Tab. 1 where is shown the full database concerning the epochs for which the observed ionograms over the radio link Rome-Chania were selected according to the criteria a) and b) above mentioned.

The MUF calculated by both the IONORT-IRI-WC and the IONORT-ISP-WC system, and the measured MUF for all the ionograms of the test database, are shown together with the corresponding differences between the modelled (IONORT-IRI-WC or IONORT-ISP-WC system) and the measured MUF values. From the results shown in the columns D and E, it can be seen that IONORT-ISP-WC MUF values are close to the measured values in most of the cases considered.

To better highlight the results of Tab. 1, the results of the comparison between the differences (IONORT-IRI-WC MUF – measured MUF), and (IONORT-ISP-WC MUF – measured MUF), are also presented in Fig. 5 for the whole test database. It is clearly evident that IONORT-ISP-WC system performs better than IONORT-IRI-WC system because in most of cases considered, the differences (IONORT-ISP-WC MUF – measured MUF) are very small (in particular, see in Fig. 5 the red squares ranged between the horizontal lines -0.5 – 0.5 MHz), and only in six cases (see in Fig. 5 the green squares marked with the symbol *) is the performance of IONORT-IRI-WC better than that of IONORT-ISP-WC.

4. Conclusions and future developments

The oblique ionograms synthesized by the IONORT-ISP-WC system are generally better than the oblique ionograms synthesized by the IONORT-IRI-WC system. From the analysis conducted on the whole database, it emerges that the IONORT-ISP-WC MUF values are more accurate than the IONORT-IRI-WC MUF values (see Tab. 1 and Fig. 5). As expected, this means that the representation of the ionosphere produced by the ISP model is more realistic than the climatological representation produced by the IRI model, and also that the ray-tracing results performed by the IONORT algorithm are reasonably reliable.

Nevertheless, Tab. 1 and Fig. 5 show also some cases for which the MUF values provided by the IONORT-ISP-WC system are greatly underestimated, on 8 October 2011 at 19: 00 UT and, most noticeably, on 8 October 2011 at 10.30 UT, or overestimated, on 6 July 2011 at 12:00 UT, and 9 October 2011 at 05:00 and 06:30 UT. In these cases no data was available from Rome and Gibilmanna, and the only reference ionospheric station contributing to the ISP grids was Athens. This estimate of MUF values provided by the IONORT-ISP-WC system could probably be smoothed out by including additional ionospheric reference stations in the region of interest, and especially located around the midpoint of the path considered.

It is also worth noting that the comparison of the synthesized ionograms with or without the collisional model used in this study (see for example Figs. 3 and 4), shows that during daytime, for the lower ionospheric layers, the traces of the synthesized ionograms are cut away at low frequencies; during night-time, when the lower ionospheric layer are missing and the absorption is not important, the traces of the simulated ionograms for the higher ionospheric layers are not cut off at low frequencies. These results provide a further confirmation about the goodness of the IONORT-ISP-WC system in providing consistent results.

In summary, the results presented in this paper suggest that: a) the assimilation of data measured at multiple ionospheric reference stations by ISP is very important to obtain as reliable an image of the ionosphere as possible; b) the IONORT-ISP-WC system can be proposed as a valid tool for operational use.

With regard to future developments, the IONORT-ISP-WC system does not provide a procedure to compute the horizontal gradients of the ionosphere, although the electron density profile grids are now characterized by a denser resolution in the latitude and longitude coordinates, i.e. from $2^{\circ}x2^{\circ}$ to $1^{\circ}x1^{\circ}$. This issue will be addressed in the future by developing a procedure capable of taking the presence of horizontal gradients into account, in order to improve the IONORT-ISP-WC system.

Moreover, more oblique sounding measurements will need to be conducted in order to investigate the issue of the underestimates/overestimates of MUF values and further test the behaviour of the IONORT-ISP-WC system.

Acknowledgments

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Figure 1. Semi-logarithmic plot of the electron collision frequency ν, in units of s^{-1}, as a function of height above ground h, in the range 50 – 250 km obtained from Eq. 1.

Figure 2. Graphical user interface of IONORT program. The 2-D and 3-D visualizations of the ray paths are shown at the bottom and right respectively, considering a transmitter point at Rome and an azimuth angle of transmission equal to 121.6° (direction of Chania), on 26 June 2011 at 01:00 UT. To realize the full potential of IONORT, composite simulations, based on the global IRI model, are performed not only inside but also outside the central Mediterranean region, by taking the geomagnetic field and the electron collisions into account, with single or multiple ionospheric reflections (1 – 3 hop paths): for a fixed elevation angle of 18° with a 3 MHz frequency-step procedure from 3 MHz to 30 MHz; and for a fixed frequency of 15 MHz with a 5° elevation-step procedure from 0° to 60°.

Figure 3. A comparison between the oblique ionogram recorded over the Rome-Chania radio link on 07 July 2011 at 15:00 UT (top panel), and the corresponding ionograms synthesized by the IONORT-IRI-WC (middle panel) and IONORT-ISP-WC (bottom panel) system. The red and purple vertical lines indicate the MUF values for the 1-hop and 3-hop paths respectively. The LOF values are also indicated for the E and F regions. For the sake of clarity, only the ordinary trace computed taking the geomagnetic field into account is shown. Both with single and multiple ionospheric reflections (1 – 3 hop paths), a nested loop cycle was iterated with azimuth angles from 121° to 122° of step 0.2°. The elevation angle step was set to 0.2° and the RX range accuracy to 0.1 %. The ionograms calculated without applying the collisional model of Eq. 1, labelled with NC are also shown for a further comparison.

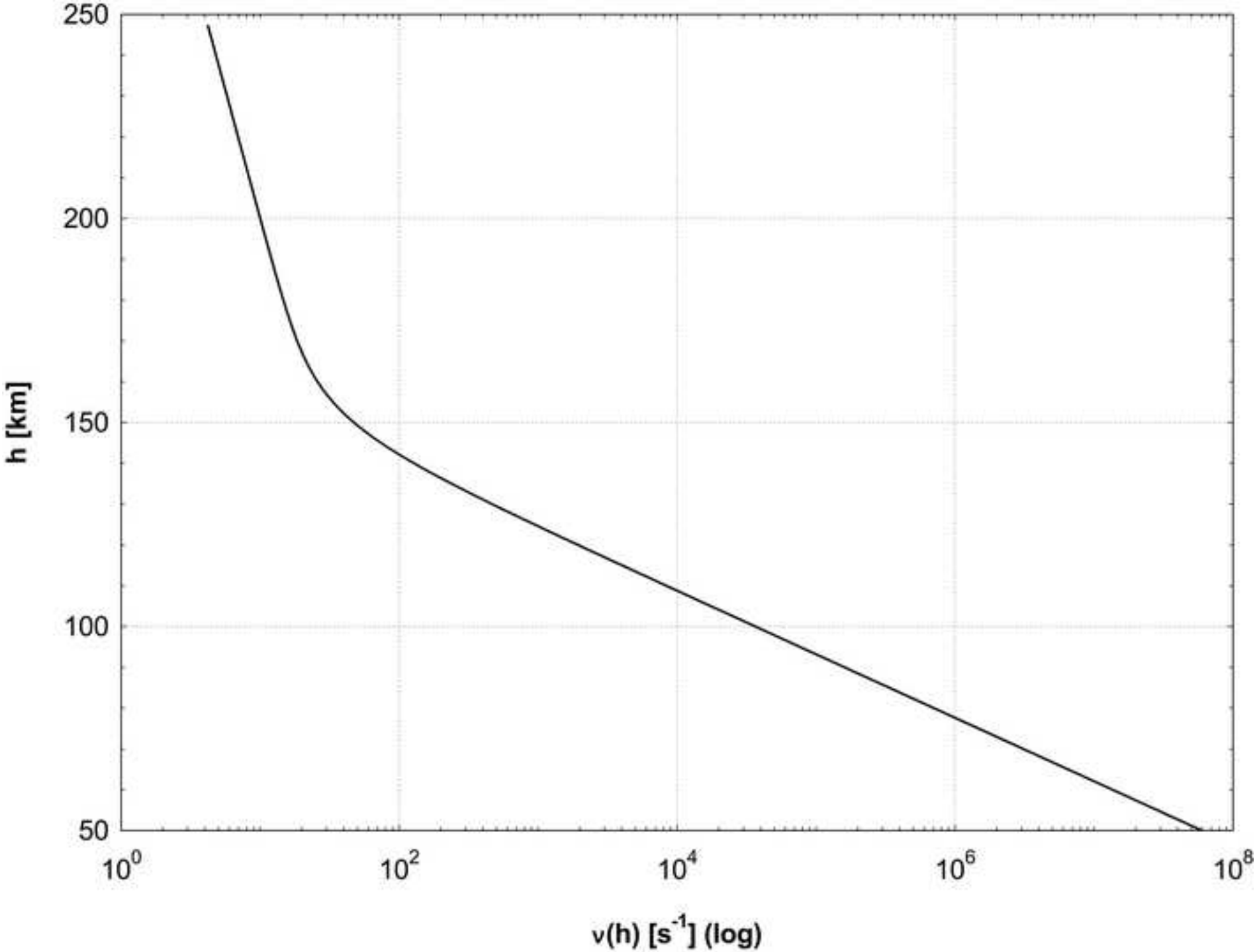
Figure. 4. Same as in Fig. 3. A comparison is shown between the ordinary traces of the oblique ionograms recorded over the Rome-Chania radio link on 09 October 2011 at 03:00 UT (top panel,

on the left), and 26 June 2011 at 01:00 UT (top panel, on the right), and the corresponding ionograms synthesized by the IONORT-IRI-WC (middle panels) and IONORT-ISP-WC (bottom panels) system. The ionograms calculated without applying the collisional model of Eq. 1, labelled with NC are also shown for a further comparison.

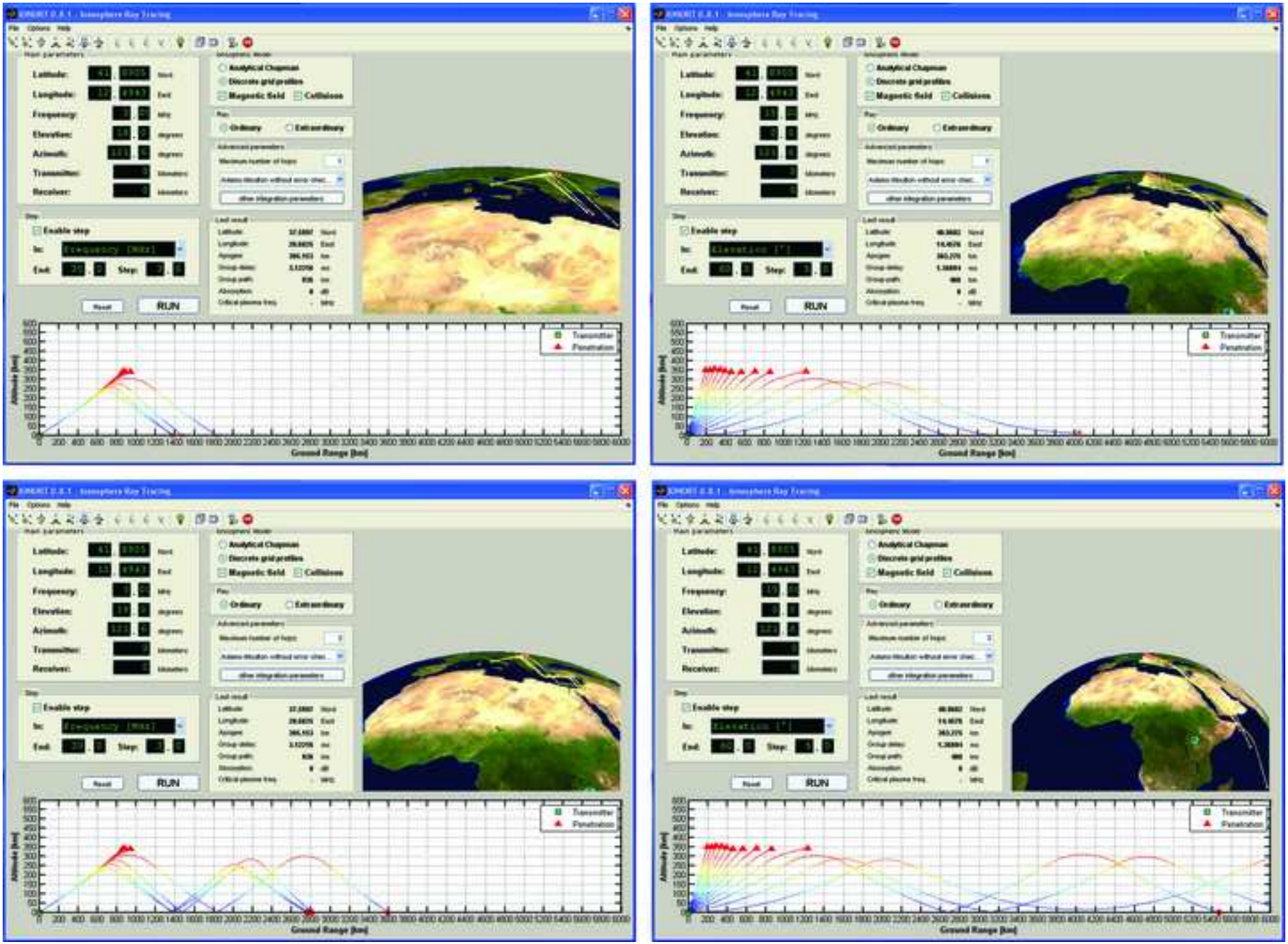
Figure 5. Comparisons between the differences (IONORT-IRI-WC MUF – measured MUF) (green squares) and (IONORT-ISP-WC MUF – measured MUF) (red squares) for the whole test database. The arrows indicate the cases for which the IONORT-ISP-WC system mostly underestimates/overestimates the MUF values. The symbol * marks the 6 cases for which IONORT-IRI-WC system performs better than IONORT-ISP-WC system.

Table 1. The MUF values calculated by the IONORT-IRI-WC system (column A), the MUF values calculated by the IONORT-ISP-WC system (column B), the measured MUF values (column C), the differences IONORT-IRI-WC MUF – measured MUF (Δ_{IRI}, column D) and IONORT-ISP-WC MUF – measured MUF (Δ_{ISP}, column E) are shown for all the ionograms in the test database. For each epoch, the lowest difference in absolute value between the modelled MUF (IONORT-IRI-WC or IONORT-ISP-WC) and the measured MUF is highlighted in bold.

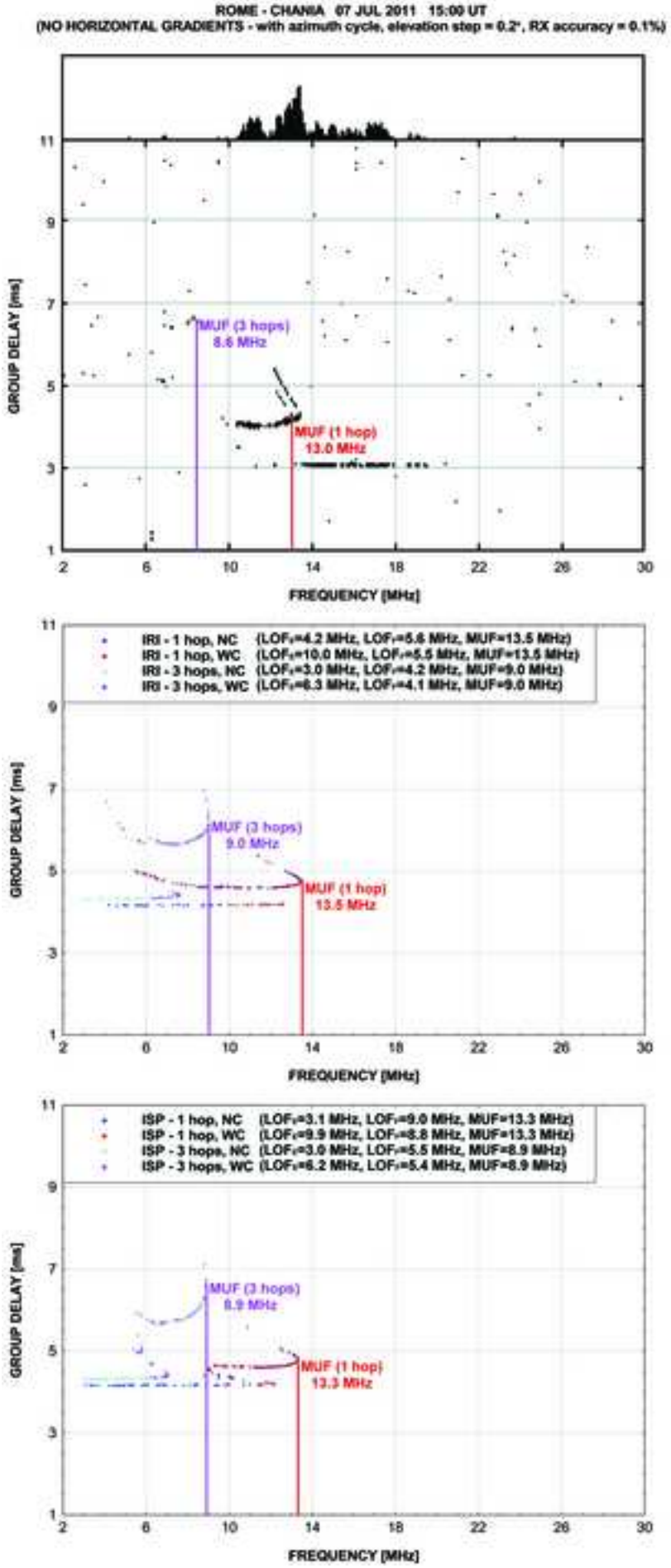
NEW_Figure_1



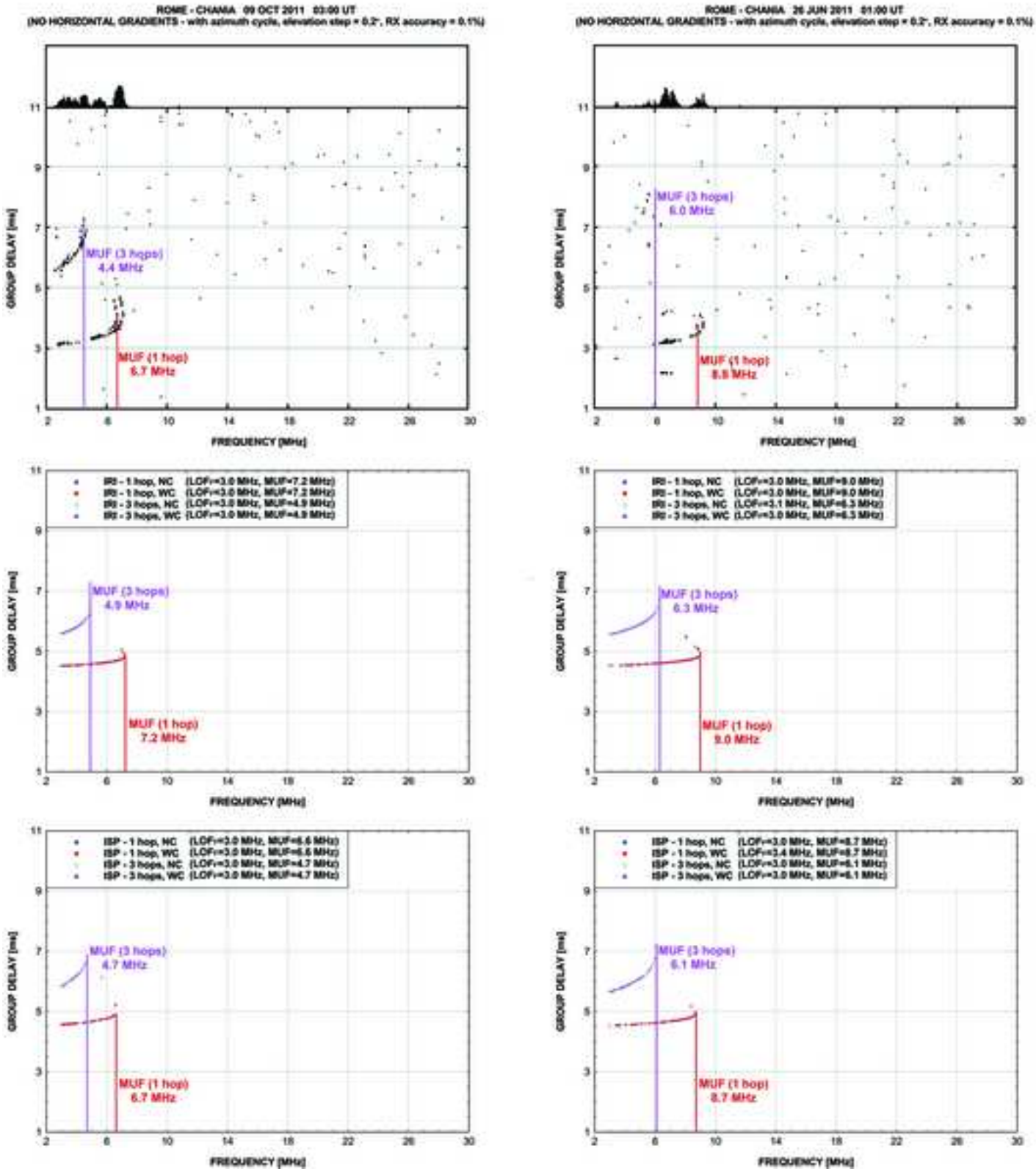
NEW_Figure_2


Analytical Chapman
Discrete grid profiles
Magnetic field
Collisions
Ordinary
Extraordinary
Enable step
RUN
Transmitter
Penetration
Ground Range [km]

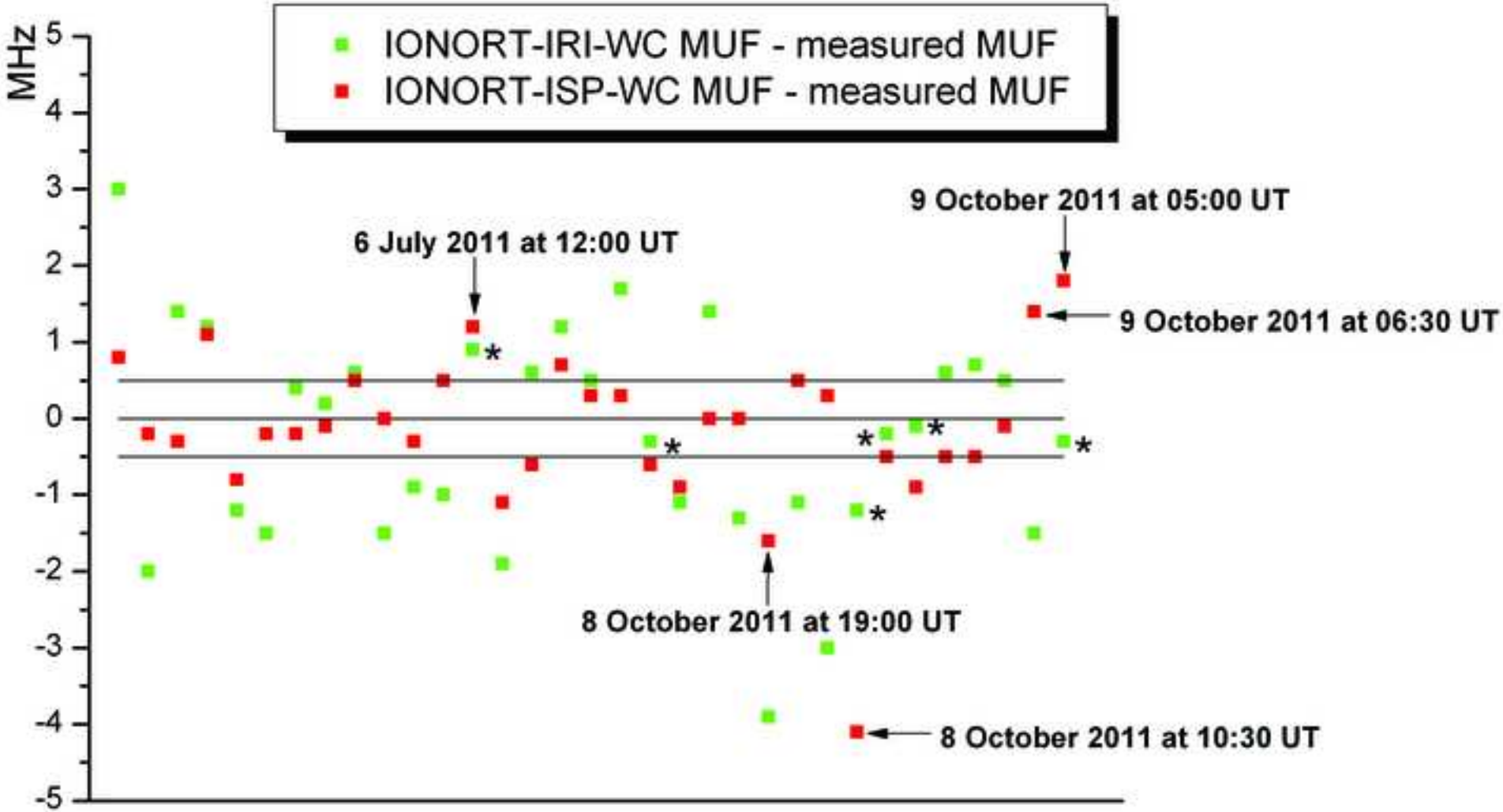
NEW_Figure_3


ROME - CHANIA 07 JUL 2011 15:00 UT
(NO HORIZONTAL GRADIENTS - with azimuth cycle, elevation step = 0.2°, RX accuracy = 0.1%)
GROUP DELAY [ms]
FREQUENCY [MHz]
MUF (3 hops)
8.6 MHz
MUF (1 hop)
13.0 MHz
IRI - 1 hop, NC (LOF1=4.2 MHz, LOF2=5.6 MHz, MUF=13.5 MHz)
IRI - 1 hop, WC (LOF1=10.0 MHz, LOF2=5.5 MHz, MUF=13.5 MHz)
IRI - 3 hops, NC (LOF1=3.0 MHz, LOF2=4.2 MHz, MUF=9.0 MHz)
IRI - 3 hops, WC (LOF1=6.3 MHz, LOF2=4.1 MHz, MUF=9.0 MHz)
MUF (3 hops)
9.0 MHz
MUF (1 hop)
13.5 MHz
ISP - 1 hop, NC (LOF1=3.1 MHz, LOF2=9.0 MHz, MUF=13.3 MHz)
ISP - 1 hop, WC (LOF1=9.9 MHz, LOF2=8.8 MHz, MUF=13.3 MHz)
ISP - 3 hops, NC (LOF1=3.0 MHz, LOF2=5.5 MHz, MUF=8.9 MHz)
ISP - 3 hops, WC (LOF1=6.2 MHz, LOF2=5.4 MHz, MUF=8.9 MHz)
MUF (3 hops)
8.9 MHz
MUF (1 hop)
13.3 MHz

NEW_Figure_4


ROME - CHANIA 09 OCT 2011 03:00 UT
(NO HORIZONTAL GRADIENTS - with azimuth cycle, elevation step = 0.2°, RX accuracy = 0.1%)
GROUP DELAY [ms]
FREQUENCY [MHz]
MUF (3 hops)
4.4 MHz
MUF (1 hop)
6.7 MHz
ROME - CHANIA 26 JUN 2011 01:00 UT
(NO HORIZONTAL GRADIENTS - with azimuth cycle, elevation step = 0.2°, RX accuracy = 0.1%)
GROUP DELAY [ms]
FREQUENCY [MHz]
MUF (3 hops)
6.0 MHz
MUF (1 hop)
8.8 MHz
IRI - 1 hop, NC (LOFv=3.0 MHz, MUF=7.2 MHz)
IRI - 1 hop, WC (LOFv=3.0 MHz, MUF=7.2 MHz)
IRI - 3 hops, NC (LOFv=3.0 MHz, MUF=4.9 MHz)
IRI - 3 hops, WC (LOFv=3.0 MHz, MUF=4.9 MHz)
GROUP DELAY [ms]
FREQUENCY [MHz]
MUF (3 hops)
4.9 MHz
MUF (1 hop)
7.2 MHz
IRI - 1 hop, NC (LOFv=3.0 MHz, MUF=9.0 MHz)
IRI - 1 hop, WC (LOFv=3.0 MHz, MUF=9.0 MHz)
IRI - 3 hops, NC (LOFv=3.1 MHz, MUF=6.3 MHz)
IRI - 3 hops, WC (LOFv=3.0 MHz, MUF=6.3 MHz)
GROUP DELAY [ms]
FREQUENCY [MHz]
MUF (3 hops)
6.3 MHz
MUF (1 hop)
9.0 MHz
ISP - 1 hop, NC (LOFv=3.0 MHz, MUF=6.6 MHz)
ISP - 1 hop, WC (LOFv=3.0 MHz, MUF=6.6 MHz)
ISP - 3 hops, NC (LOFv=3.0 MHz, MUF=4.7 MHz)
ISP - 3 hops, WC (LOFv=3.0 MHz, MUF=4.7 MHz)
GROUP DELAY [ms]
FREQUENCY [MHz]
MUF (3 hops)
4.7 MHz
MUF (1 hop)
6.7 MHz
ISP - 1 hop, NC (LOFv=3.0 MHz, MUF=8.7 MHz)
ISP - 1 hop, WC (LOFv=3.4 MHz, MUF=8.7 MHz)
ISP - 3 hops, NC (LOFv=3.0 MHz, MUF=6.1 MHz)
ISP - 3 hops, WC (LOFv=3.0 MHz, MUF=6.1 MHz)
GROUP DELAY [ms]
FREQUENCY [MHz]
MUF (3 hops)
6.1 MHz
MUF (1 hop)
8.7 MHz

NEW_Figure_5


IONORT-IRI-WC MUF - measured MUF
IONORT-ISP-WC MUF - measured MUF
MHz
5
4
3
2
1
0
-1
-2
-3
-4
-5
6 July 2011 at 12:00 UT
9 October 2011 at 05:00 UT
9 October 2011 at 06:30 UT
8 October 2011 at 19:00 UT
8 October 2011 at 10:30 UT

NEW_Table_1

Epoch	A IONORT-IRI-WC MUF [MHz]	B IONORT-ISP-WC MUF [MHz]	C MEASURED MUF [MHz]	D Δ_{IRI} [MHz]	E Δ_{ISP} [MHz]
23 JUN 2011 - 17:00	13.7	11.5	10.7	3.0	**0.8**
23 JUN 2011 - 19:00	12.9	14.7	14.9	-2.0	**-0.2**
23 JUN 2011 - 23:00	10.0	8.3	8.6	1.4	**-0.3**
25 JUN 2011 - 10:00	14.6	14.5	13.4	1.2	**1.1**
25 JUN 2011 - 20:00	12.2	12.6	13.4	-1.2	**-0.8**
25 JUN 2011 - 23:00	9.9	11.2	11.4	-1.5	**-0.2**
26 JUN 2011 - 00:00	9.4	8.8	9.0	0.4	**-0.2**
26 JUN 2011 - 01:00	9.0	8.7	8.8	0.2	**-0.1**
26 JUN 2011 - 02:00	8.8	8.7	8.2	0.6	**0.5**
03 JUL 2011 - 17:00	13.6	15.1	15.1	-1.5	**0.0**
04 JUL 2011 - 19:00	12.9	13.5	13.8	-0.9	**-0.3**
04 JUL 2011 - 20:00	12.2	13.7	13.2	-1.0	**0.5**
06 JUL 2011 - 12:00	14.6	14.9	13.7	**0.9**	1.2
06 JUL 2011 - 21:00	11.6	12.4	13.5	-1.9	**-1.1**
07 JUL 2011 - 01:00	8.9	7.7	8.3	0.6	-0.6
07 JUL 2011 - 14:00	13.6	13.1	12.4	1.2	**0.7**
07 JUL 2011 - 15:00	13.5	13.3	13.0	0.5	**0.3**
07 JUL 2011 - 17:00	13.5	12.1	11.8	1.7	**0.3**
07 JUL 2011 - 18:00	13.2	12.9	13.5	**-0.3**	-0.6
07 JUL 2011 - 19:00	12.9	13.1	14.0	-1.1	**-0.9**
08 JUL 2011 - 17:00	13.5	12.1	12.1	1.4	**0.0**
08 JUL 2011 - 18:00	13.2	14.5	14.5	-1.3	**0.0**
08 JUL 2011 - 19:00	12.8	15.1	16.7	-3.9	**-1.6**
08 OCT 2011 - 06:15	14.8	16.4	15.9	-1.1	**0.5**
08 OCT 2011 - 06:45	14.7	18.0	17.7	-3.0	**0.3**
08 OCT 2011 - 10:30	19.3	16.4	20.5	**-1.2**	-4.1
08 OCT 2011 - 20:00	9.0	8.7	9.2	**-0.2**	-0.5
08 OCT 2011 - 23:45	7.6	6.8	7.7	**-0.1**	-0.9
09 OCT 2011 - 02:00	7.5	6.4	6.9	0.6	**-0.5**
09 OCT 2011 - 02:15	7.5	6.3	6.8	0.7	**-0.5**
09 OCT 2011 - 03:00	7.2	6.6	6.7	0.5	**-0.1**
09 OCT 2011 - 05:00	10.7	13.6	12.2	-1.5	**1.4**
09 OCT 2011 - 06:30	14.8	16.9	15.1	**-0.3**	1.8