Effects of geological complexities on coseismic displacement: hints from 2D numerical modelling

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Abstract

By means of a 2D finite-element procedure, we test how heterogeneities at the scale of seismogenic fault affect the displacement. We define one or more slip distributions for two typical normal-faulting earthquakes in the Central Apennines, compute the displacement occurred within different structures, including lateral heterogeneities, and compare the different displacement profiles in order to isolate the effect of the crustal structure. To understand at what magnitude the heterogeneities affect significantly the observation, we compare the predicted coseismic displacement with GPS and DInSAR data for the Colfiorito 1997 earthquake. We find that heterogeneities significantly affect the observable horizontal coseismic displacement for the larger magnitudes, whereas for smaller quakes they affect horizontal displacement close to the fault trace only.

Keywords

fault, numerical models, displacements, heterogeneity, Colfiorito
1. Introduction

Surface displacement induced by faults has been studied at different scales, from the fine structure of the fault zone to the crustal heterogeneities, depending on the observation scale and on the specific problem (see, e.g., Guðmundsson and Brenner, 2003; Zhao et al., 2004). Earthquakes provide us with seismological data to study the causative fault at depth and a sudden displacement at the surface – the effect. Due to poor sampling of data, the coseismic displacement has been often computed assuming homogenous or layered models for the crustal structure in both analytic and finite-element methods. When the data are scarce or inaccurate or when the stratification is poorly known, using simpler models improves the robustness of results obtained by vertical measurements. Differently, horizontal displacements are very sensitive to the presence of low-rigidity layers (Savage, 1998; Cattin et al., 1999; Zhao et al., 2004). As a consequence, wrong fault parameters and slip distribution may derive from inversion of measured displacement when the wrong layering is used.

Today, denser GPS networks of improved technology provide a number of observations of the horizontal displacement. The analysis of these GPS data, separately from or jointly with DInSAR, requires more detailed modelling of the crustal structure, of the earthquake fault, and of the slip distribution. For a 2-D dip-slip fault, we study surface displacements due to different slip distributions and assuming different approximations of the crustal structure.

As a study case, we choose the 1997-98 normal-faulting Colfiorito earthquakes (Central Apennines mountain belt, Italy, Fig. 1), where data disagrees from interpretations (Barba and Basili, 2000). The belt also exhibits horizontal and vertical heterogeneities in the stratification at the length scale of seismogenic faults (Mirabella and Pucci, 2002; Chiarabba and Amato, 2003). The availability of detailed seismic profiles, the occurrence of shallow moderate-magnitude earthquakes, a good record of historical and instrumental earthquakes (up to M7.0, CPTI Working Group, 2004), the long term geological, seismological, and geodetic surveying, and the vast literature available in
the area (Amato and Cocco, 2000, and references therein) provide us a good framework to test how
the heterogeneous medium affects the observations.

2. Modelling approach

We build four models with different lithologies assuming uniform slip, and then use several
normalized slip distributions in the most complex model to represent how slip distribution
influences displacement, accounting also for the fault damage zone. We model two faults capable of
typical normal-faulting earthquakes, one large (M6.7), and the other moderate (M6).

2.1 Finite element model

We build the two-dimensional finite-element mesh in a vertical section across the fault by
reproducing the detailed geological section of Mirabella and Pucci (2002) (Fig. 2a), using the code
MSC.Marc (MSC.Software, 2006).

To isolate the effect of the main seismogenic fault, we reproduce the section including only
the most important interfaces. We consider as important such objects (interfaces, lithologies …)
whose length is at least 1/10th of the seismogenic fault down-dip width (W), and are located close to
the fault. We will show that the smallest heterogeneities we accounted for – the turbidites layer - do
not affect results. Thus we neglect, as details, smaller heterogeneities and smooth the geometry off
of the fault (Fig. 2b). From the section we can easily identify four major lithologic units. From top
to bottom, they are Miocene Plio-Pleistocene turbidites, Meso-Cenozoic carbonate multilayer,
Triassic evaporites, and a Phyllitic Permian-Triassic basement.

The modelled section (300 km length, 100 km depth) has been meshed with four-node
quadrilaterals (11,452 elements and 11,735 nodes) (Fig. 2c). The fault lies entirely within the
computational domain and cuts the mesh with zero friction slipping edges. Out of the fault zone,
surface displacement depends on the final slip and not on friction, and depends very little on the
gouge thickness. As for the boundary conditions, the upper surface acts as a stress-free boundary,
whereas the left, right, and bottom edges of the model have been assigned zero displacement in the normal direction.

Our procedure uses variable magnitude forces on the nodes along the fault and orthogonal reaction forces so that the total torque is near zero, as described in Megna et al. (2005): the modelled displacement compares well (~5%) to the analytical solution close to the fault trace, i.e. where measures exist, which validates our procedure.

In the Model1, we consider a top layer with average carbonates-evaporites elastic parameters (CA-EV in Table 1) and the basement; in the models 2-4 we use the evaporites and not the average layer; in Model2 we include the carbonates at the top of the evaporites; in Model3 we add the turbidites over the evaporites; in Model4 we incorporate the lateral heterogeneities due to the thrusting (Fig. 3).

Based on P- and S-wave velocity from the literature, we adopt a Young modulus in the range of 8-83 GPa (Table 1). Unfortunately, we do not have access to laboratory values; but we verified that in the South Iceland Seismic Zone in-situ measurements close to the fault yield Young moduli in the lower range of ours (5-10 GPa, Gudmundsson and Brenner, 2003), and the range of seismic velocities is similar (Tryggvason et al., 2002). To account also for such low measurements, we also include in Model4 a fault damage zone (400 m thick, Y=5-10 GPa).

2.2 Fault parameters

We studied the normal fault of Colfiorito, ruptured during the 1997-98 earthquake sequence. The CMT fault-plane solution of 26 September 1997 mainshock indicates almost pure normal faulting along a ~40° plane dipping toward SW (Ekström et al., 1998). The aftershocks depth distribution is confined between 2 and 9 km (Barba and Basili, 2000; Chiarabba and Amato, 2003), therefore affecting the carbonate multilayer and the evaporites but not the basement (Collettini and Barchi, 2002). Considering these constraints, we define a fault with a dip of 40°, which dislocates the carbonates and evaporites, and its bottom is just over the basement top. We define the two different magnitudes (M6 and M6.7) by setting different fault down-dip width (W=7 and 10 km).
To define the slip, we select arbitrarily some slip distributions in the literature and scale them over the assigned W by using standard relationships (Hanks and Kanamori, 1979; Aki and Richards, 2002) with L/W=1.5-2 and μ=23 GPa (this work) for the Central Apennines.

For the M6.7 earthquake, we consider four slip distributions: uniform slip (US), not uniform slip due to fault-parallel couples of uniform forces acting on the footwall and hanging wall (UF), step-like slip (SL), and symmetrical slip distribution with the maximum value in the centre (CE) (Fig. 4a). All the distributions share the same average slip of 1 m. From the top to the bottom of the fault, we set the slip for SL as 0.4 m (0.8 m; 1.6 m) in a 3 km wide segment (3 km; 4 km); for CE as 0.6 m (1.6 m, 0.6 m) in a 3 km segment (4 km; 3 km), all with the fault top Zt=1 km depth.

For the M6 earthquake, we consider results available in the literature for the Colfiorito earthquake. By inverting geodetic data, many authors (see, e.g., Belardinelli et al., 2004; Hernandez et al., 2004; Lungdren and Stramondo, 2004; Santini et al., 2004) found an asymmetric slip distribution, with the maximum located in the lower half of the fault. For most of them, W ranges between 9 and 10 km, Zt~1 km depth, and the slip averages to ~ 0.4 m. Differently, earthquake locations show that very few or no aftershocks have been reliably located at less than 2 km depth, despite the dense coverage of temporary seismic stations in the area, and that the fault width ranges W~7.5 km (Barba and Basili, 2000) to W~10 km (Chiarabba and Amato, 2003). By analysing the near-source strong motion data of the main shock, Zollo et al. (1999) found W=7.5 km, and a nearly uniform slip along the fault – except at the tips of the fault, where the slip rapidly decreases. Considering these constraints, we define for M6 three slip distributions (W=7-10 km, Zt=1-2 km, slip distributions US, AV, TR) with average slip 0.4 m, as showed in figure 4b. In particular, we computed the average slip distribution (AV) from Hernandez et al. (2004) and Santini et al. (2004).
3. Results

3.1 Case of Magnitude 6.7

We characterise our synthetic case for a M6.7 earthquake with a fault whose parameters are \( W=10 \text{ km}, Z_t=1 \text{ km} \), and the slip distributions US, UF, CE, and SL with average slip \( \sim 1 \text{ m} \).

Comparing the results obtained by fixing the slip distribution US, the horizontal displacement shows variations ranging from 18\% to 49\% (with the top depth between 1 km and 3 km) (Fig. 5, \( Z_t=1 \text{ km} \) case only), causing even greater extension or shortening, as the sign changes across the fault trace. Most of the variation takes place in Model3 and Model4, and it depends by the presence of the low-Young moduli layers at shallow depths. The vertical displacement instead shows some difference (\( \sim 16\% \)) among the different models 1-4, especially at the maximum subsidence. Contrary to models 1-3, the heterogeneous Model4 exhibits maximum uplift in the footwall.

To understand the effect of the slip in the most complex Model4, we compare the displacements obtained by the slip distributions US, UF, CE, and SL; the vertical displacement pattern due to UF and CE moves to the left and produces a deeper subsidence than US (Fig. 6a). On the contrary, SL pattern shifts more, predicts \( \sim 20\% \) less subsidence, and shows longer wavelength than US. The horizontal displacement yields similar results: when the maximum of the slip distribution moves towards the bottom of the fault, the peaks in the horizontal displacement move away from the fault trace, and the wavelength increases (6b).

3.2 Case of Magnitude 6 and comparison with geodetic data

The main question is whether the effect of the crustal model onto the surface displacement can be observed with GPS and/or DInSAR data. We base our M6 synthetic case on the Colfiorito 1997 earthquake, as described in section 2.2. For the three slip distributions, we compare the displacement computed in Model1 and heterogeneous Model4. Results show that the presence of heterogeneities causes little increase of (\( \sim 1 \text{ or } 2 \text{ cm} \)) footwall uplift (Fig. 7a, US case only). For the subsidence instead the results depend on the slip distribution; the subsidence decreases \( \sim 1 \text{ cm} \) for US, remains unchanged for AV, and increases \( \sim 2 \text{ cm} \) for TR. Figure 7b shows the different patterns.
of the vertical displacement for the three slip distributions in the case of heterogeneous Model4. Imposing the slip AV or TR, the maximum subsidence moves toward the left direction, and its value increases up to ~30% (~6 cm) with respect to US. The uplift due to AV and TR increases on the hanging wall with respect to US, whereas it does not change above the footwall.

As for the horizontal displacement, the heterogeneities present in Model4 make the extension across the fault trace to increase significantly, like in the M6.7 case (Fig. 8a). For the cases of US and AV, the horizontal displacement increases by ~40% in the footwall and ~15% (1 cm) in the hanging wall. For the TR case, we find ~67% on the footwall and ~27% (2 cm) on the hanging wall. Focusing on Model4, we observe that the cases US, AV, and TR induce a large difference in the horizontal displacement mainly in the hanging wall (Fig. 8b) both in amplitude and wavelength.

We compare the computed displacement with the GPS and DInSAR data recorded in the Colfiorito zone after three moderate magnitude earthquakes (Salvi et al., 2000). The satellite line of sight is near to vertical (~23°), thus we approximate DInSAR data as vertical. In order to partly separate the effect of the three events in the GPS data, we consider only the stations close to the center of the largest fault: PENN (footwall) and CROC (hanging-wall). For the DInSAR data, we make a 4 km-wide box selection across the fault and located in the maximum subsidence zone. In several papers, the final models hardly predict the horizontal displacement at the closest GPS stations, as it is showed in Figure 8a for the model proposed by Hernandez et al. 2004. In particular, the homogeneous model predicts a horizontal displacement that is ~50% of observed data at PENN station, which makes the authors to hypothesise a very shallow fault. Differently, we propose that such high values in the measured horizontal displacement may depend on the crustal model. In fact, we show that the presence of the heterogeneities due to thrusting and the use of realistic elastic parameters affect the horizontal displacement by a quantity (up to 100%) that can compensate the misfit obtained in less realistic models (Figs 8a and 8b). We verify that lower Young moduli (5-10 GPa) in the fault damage zone produce ~25% less horizontal displacement at the surface (Fig. 8b): more slip is required to fit the GPS measurements and, as a consequence, the effect of the more
rigid layer increases. Our results suggest that the horizontal displacement strongly depends on the heterogeneities present at depth and that GPS data are likely to show this effect. Differently, large measurement errors (~2.8 cm, Stramondo et al., 1999), mostly due to topography (<0.7 cm) and atmospheric effects (1.4 cm, Crippa et al., 2006), prevent us from discriminating among models by using DInSAR (Figs. 7a and 7b).

4. Conclusions

For a typical dip-slip fault in the Central Apennines, we study how the lithological complexities of the crust structure affect surface displacement comparing results obtained in different layered models. We show that the horizontal displacement for the tested fault geometry strongly depends on the elastic stratification, whereas the vertical component does not. This behaviour is also discussed by Savage (1998), Cattin et al. (1999), and Zhao et al. (2004). By applying different slip distributions, the displacement pattern changes in amplitude and wavelength. When lateral heterogeneities are included, the surface-displacement increases and assumes a shorter wavelength with respect to the layered models, especially in proximity of the fault trace. The position of the maximum subsidence moves towards the hanging wall when different and deeper slip distributions are considered. The wavelength increases when the slip concentrates at depth. The presence of the fault damage zone reduces the expected displacement at the surface, and requires a higher slip to fit the GPS measurements close to the fault trace. Despite the results have been obtained in a 2D model, we carried out our analysis with the data measured close to the fault trace, where 2D and 3D models do not differ significantly. The same conclusions hold for a reverse fault, and can be drawn by reversing the sign of the displacement.

We conclude that for a hypothetical shallow M6.7 earthquake, the heterogeneities significantly affect the surface displacement and have to be accounted for also in the inversion of geodetic data. On the contrary, for a M6 earthquake, the effects on the vertical displacement may be neglected, whereas on the horizontal displacement they may be very subtle and strongly dependent
on the fault depth. We show that the heterogeneities have to be carefully considered in the case of GPS stations close to the fault trace and shallow faults. By neglecting the heterogeneities in such a case, the resulting slip distribution is distorted and the fault appears to be shallower.

**References**


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Figure captions

Figure 1. Central Apennines (Italy). Surface projection of individual seismogenic faults (rectangles; DISS, 2005), thrusts, earthquakes with $M>=5.5$ (squares; CPTI, 2004), CMTs (http://www.globalcmt.org/, 2006), instrumental earthquakes (grey dots; http://www.ingv.it/~roma/reti/rms/bollettino/), GPS stations CROC and PENN (open triangles), and surface projection of EW geological section (thick line) corresponding to segment AA’ in Mirabella and Pucci (2002). In the inset, the rectangle indicates the study area.

Figure 2. (a) Geological section across Colfiorito normal fault, Central Italy (from Mirabella and Pucci, 2002); (b) geometry of the model; (c) enlargement of the mesh. In (b) and (c) the line represents the modelled fault (dashed: $W=10$ km, $Z_t=1$ km; solid: $W=7$ km, $Z_t=2$ km).

Figure 3. The different models (1-4) considered in the text. Elastic parameters are shown in table 1.

Figure 4. Slip distributions. (a) $W=10$ km, $Z_t=1$ km, solid line: SL, dashed line: US, short-dashed line: CE, dotted line: UF computed in Model4; (b) solid line: AV (Hernandez et al., 2004; Santini et al., 2004), $W=10$ km, $Z_t=1$ km; dashed line: TR (Barba and Basili, 2000; Zollo et al., 1999), $W=7$ km, $Z_t=2$ km; dotted line: US.

Figure 5. Horizontal displacement in case of US and M6.7 for models 1-4, $Z_t=1$ km, and $W=10$ km. For all the following figures, the displacement is represented at the free surface, and distances are relative to the fault trace with positive values eastwards (according to figure 1).

Figure 6. (a) Vertical and (b) horizontal displacement for US, UF, SL, CE, $W=10$ Km in Model4 ($Z_t=1$ km).

Figure 7. Vertical displacement computed for the M6 case. (a) Model1 (dashed line) and Model4 (solid line), slip distribution US, $Z_t=1$ km, $W=10$ km. (b) Model4 and slip distributions US (solid line), AV (dashed), TR (dotted). DIInSAR data (Stramondo et al., 1999; Salvi et al., 2000) (crosses; solid: reliable data, empty: unreliable; measurement error ~2.8 cm).
Figure 8. Horizontal displacement computed for the M6 case. (a) Model1 (dashed line) and Model4 (solid line) both with slip distribution AV; displacement computed using Hernandez et al. (2004) slip distribution in our Model4 (short-dashed line). (b) Model4 and slip distributions US (solid line), AV (dashed), TR (dotted), TR with Y=10 Gpa (grey dashed line). Crosses: GPS measurements at PENN and CROC sites (Salvi et al., 2000).
### Tables

**Table 1 - Elastic parameters**

<table>
<thead>
<tr>
<th>layer</th>
<th>Z (km)</th>
<th>$V_p$ (m/s)</th>
<th>$V_s$ (m/s)</th>
<th>$\rho$ (kg/m$^3$)</th>
<th>$Y$ (Pa)</th>
<th>$\nu$</th>
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<tr>
<td>turbidites</td>
<td>0-1</td>
<td>2300$^a$</td>
<td>1200$^a$</td>
<td>2300$^a$</td>
<td>8.07·10$^9$</td>
<td>0.31</td>
</tr>
<tr>
<td>carbonates</td>
<td>1-6</td>
<td>5400$^b$</td>
<td>2900$^c$</td>
<td>2600$^c$</td>
<td>5.67·10$^{10}$</td>
<td>0.30</td>
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<tr>
<td>evaporites</td>
<td>2-8</td>
<td>6300$^c$</td>
<td>3400$^c$</td>
<td>2800$^e$</td>
<td>8.38·10$^{10}$</td>
<td>0.29</td>
</tr>
<tr>
<td>basement</td>
<td>&gt;8</td>
<td>5500$^d$</td>
<td>3000$^d$</td>
<td>2840$^e$</td>
<td>6.59·10$^{10}$</td>
<td>0.29</td>
</tr>
<tr>
<td>CA-EV avg.</td>
<td>0-8</td>
<td>5850</td>
<td>2950</td>
<td>2700</td>
<td>6.94·10$^{10}$</td>
<td>0.29</td>
</tr>
</tbody>
</table>

Table 1. Parameters used in the models for the single lithologies or combination of $V_p$, $V_s$: P- and S-wave velocities; $\rho$: density; $Y$: Young’s modulus; $\nu$: Poisson’s ratio; $Z$: approximate depth range of the lithology; CA-EV: average of carbonates and evaporites. Values taken by a) Di Giulio et al., 2003; b) Morgante et al., 1998; c) Alessandrini et al., 2001; d) Barchi et al. 1998; e) Pauselli et al., 2003; f) average elastic parameters $Y$ and $\nu$ computed from $V_p$, $V_s$, and $\rho$. 
"Figure 1"
Fig. 2
Fig. 3
Fig. 4
Fig. 5
Fig. 6
Fig. 7
Fig. 8

(a) Graph showing horizontal displacement (cm) against distance (km) for different models. The models include:
- **model 4 - slip AV**
- **model 1 - slip AV**

The graph also indicates the fault damage zone and mentions model 4 - slip by Hernandez et al. (2004).

(b) Graph showing horizontal displacement (cm) against distance (km) for different materials and strains. The materials include:
- **US**
- **AV**
- **TR**

The graph indicates the fault damage zone with the modulus of elasticity Y = 10 GPa.