

Coupling of hydraulic and electrical transport properties in sandstones

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1. Introduction

- In geothermal reservoirs a characterization of the rock permeability (k) is essential and a knowledge of the permeability dependence on effective pressure (p_{eff}) is important.
- The electrical rock conductivity (σ) is significantly easier to measure both in the lab and in situ.
- Finding a link between both rock transport properties is therefore desirable.
- Such a link should exist if the rock conductivity is governed by the conductivity of a fluid within the pore space as in that case both k and σ were shown to be dependent on effective pressure.
- Scope: search suitable coupling through microstructural parameters.

2. Experimental details

Sandstone samples:



Fontainebleau



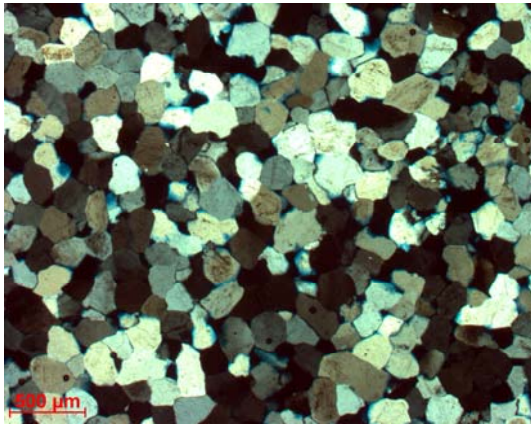
Flechtinger



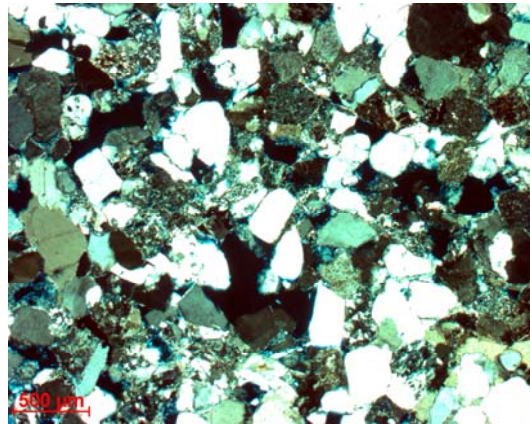
Eberswalder

Microstructure:

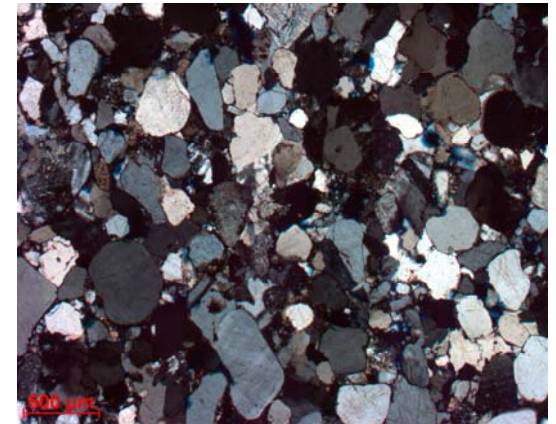
(optical, crossed nicols)



Fontainebleau



Flechtinger

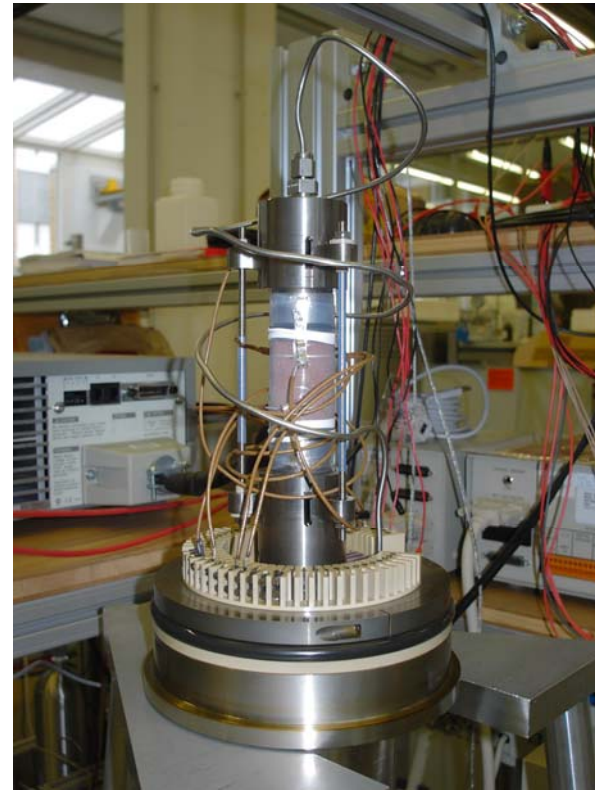


Eberswalder

Sample properties:

Sample	Porosity [%]	Permeability [mD]	Formation factor [1]
Fontainebleau	7.5	20	125
Flechtinger	9.0	0.03	38
Eberswalder	4.0	0.01	66
Fluid: 0,1 molar NaCl-solution (σ at 40°C = 13 mS/cm)			

Experimental set-up:



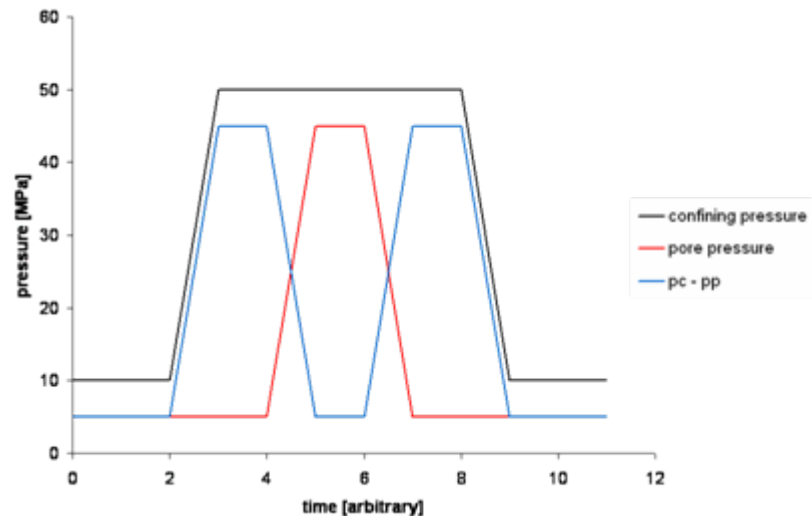
Experimental procedure:

- the experiments were performed at $T = 40 \text{ }^\circ\text{C}$
- k and σ were simultaneously measured
- effective pressure ramping was performed by successively increasing and decreasing both confining- (p_c) and pore pressure (p_p):

$p_c = [10 - 50 \text{ MPa}]$

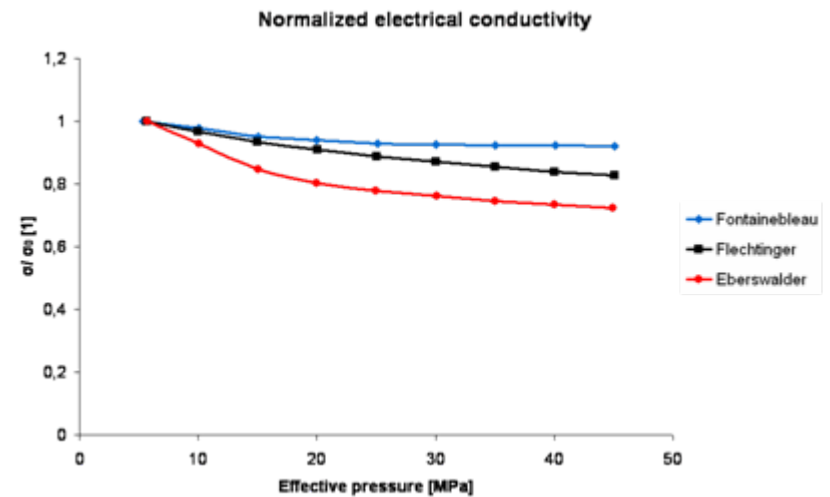
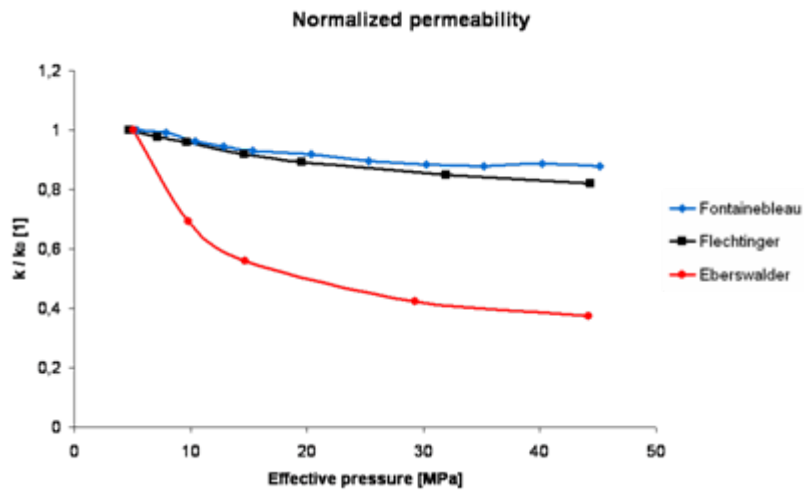
$p_p = [5 - 45 \text{ MPa}]$

Intervall = $[2.5 - 15 \text{ MPa}]$

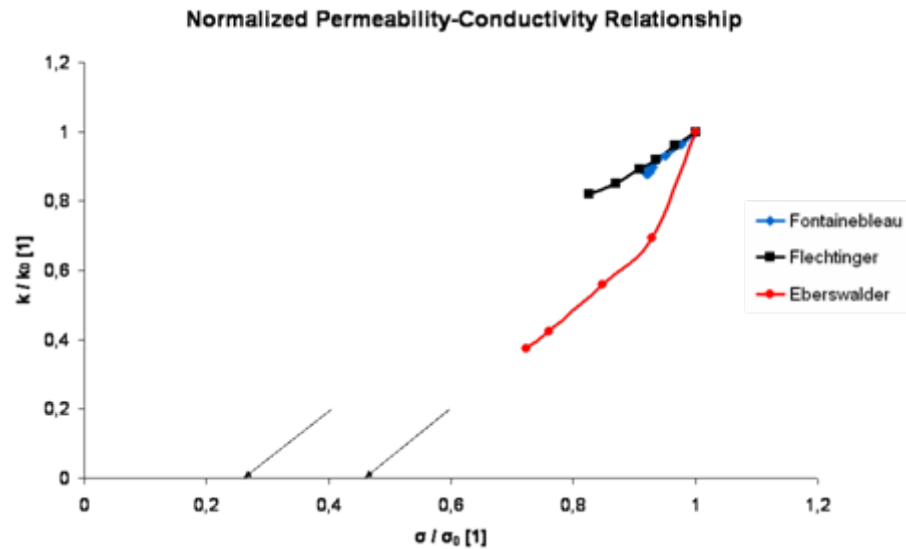


3. Experimental results

Effective pressure dependence of permeability and electrical conductivity:

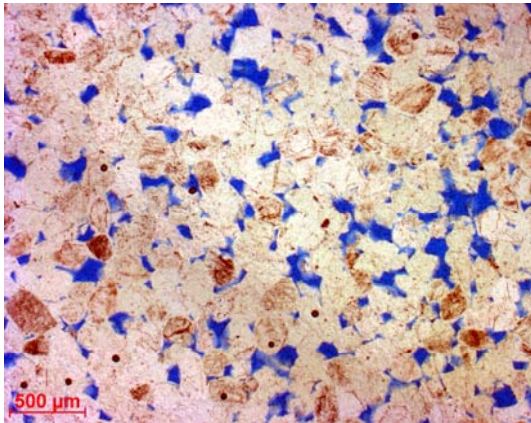


Permeability – conductivity relationship:

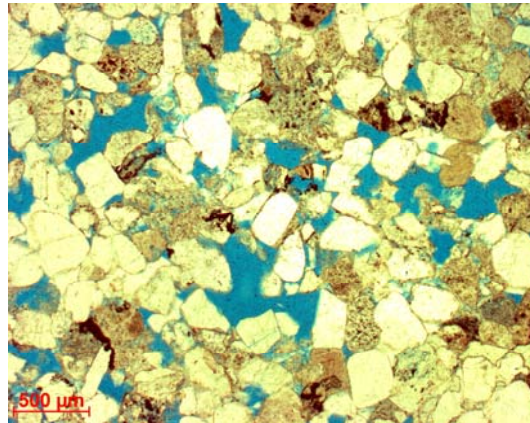


4. Microstructural analysis

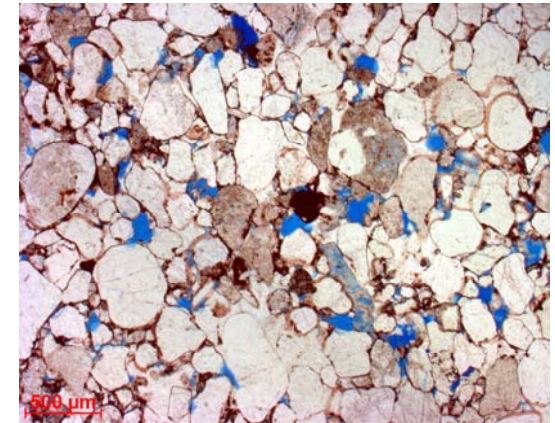
1) 2D Image Analysis:



Fontainebleau



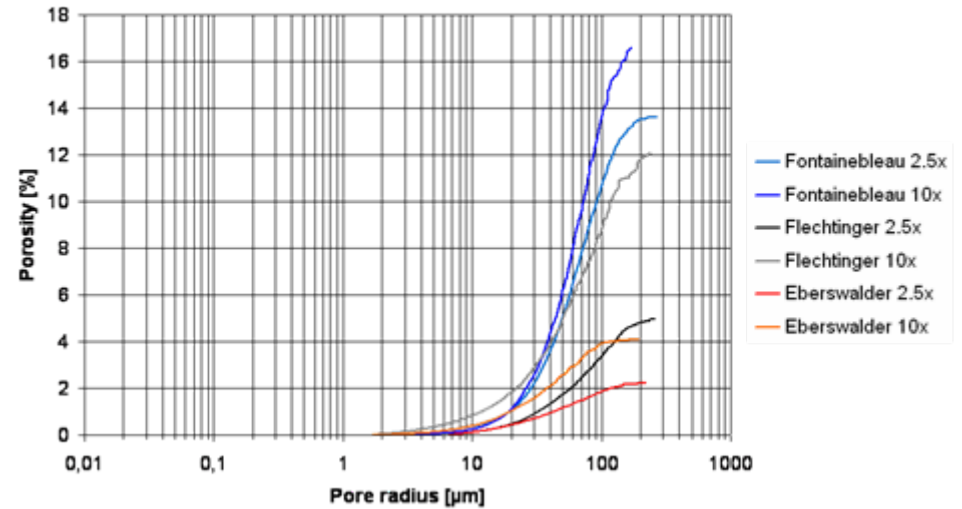
Flechtinger



Eberswalder

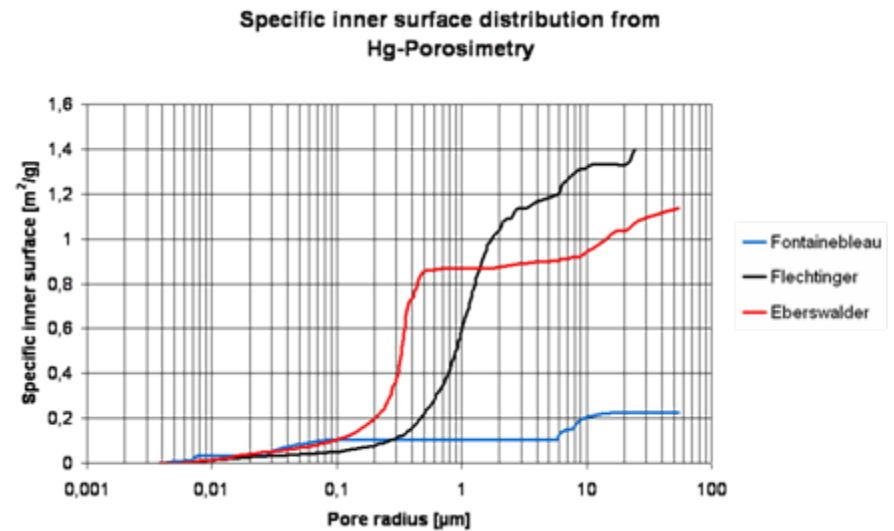
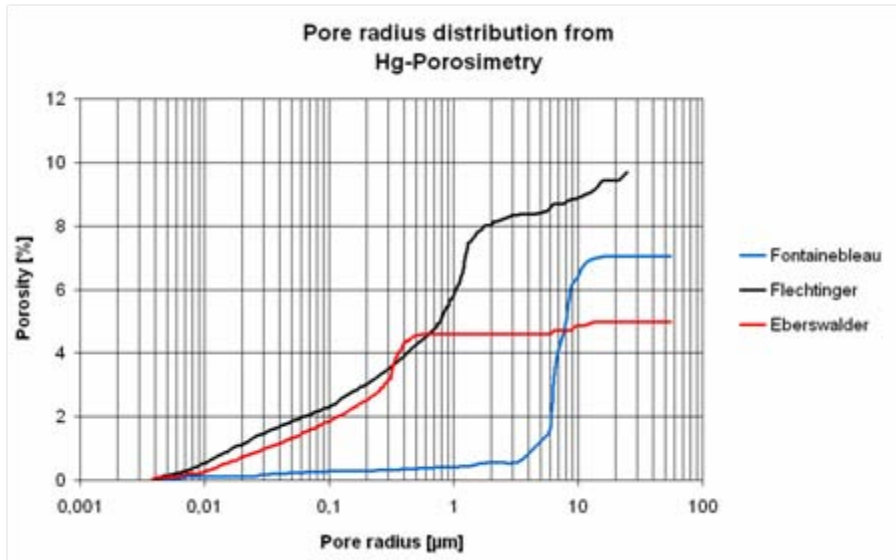
1) 2D Image Analysis (cont.):

Pore radius distribution from 2D image analysis



Sample	Average Porosity [%]	Average Pore Radius [µm]
Fontainebleau	15.1	21.7
Flechtinger	8.9	14.4
Eberswalder	3,2	12,3

2) Hg-Porosimetry:



Sample	Porosity [%]	Average Pore Radius [μm]	Specific Inner Surface [m^2/g]
Fontainebleau	7.1	7.1	0.23
Flechtinger	9.7	1.3	1.40
Eberswalder	5.0	0.4	1.14

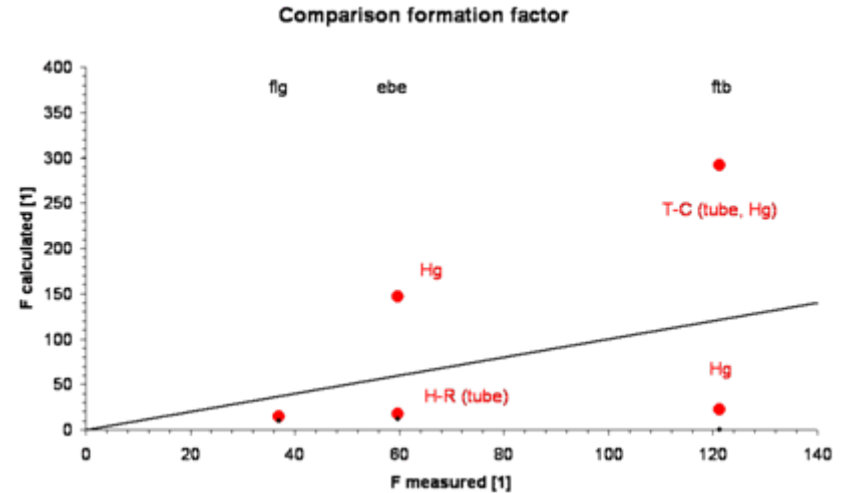
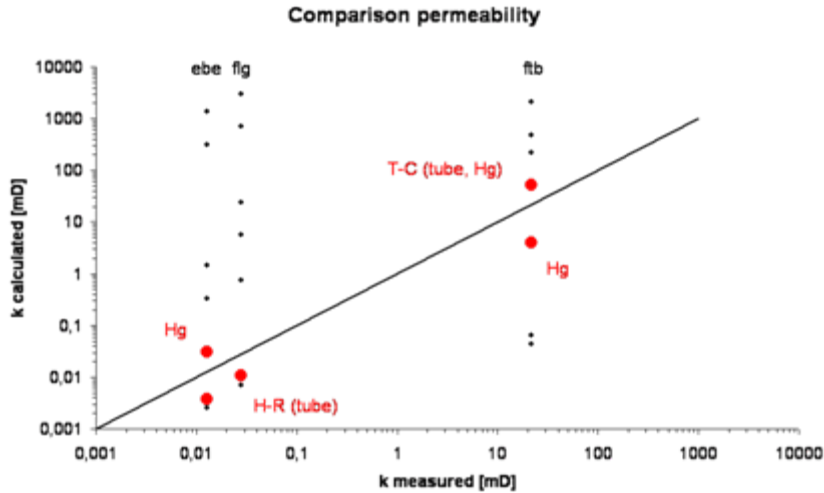
5. Integrated comparison of different scaling models

Darcy: $q = -\frac{k}{\eta} \cdot \nabla p$ Ohm: $J = -\sigma \cdot \nabla V$

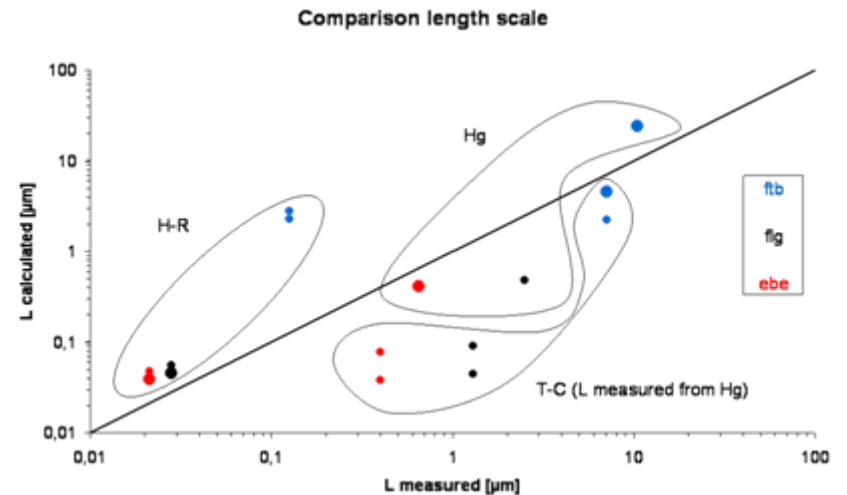
$k = c \cdot L^2 \cdot \frac{1}{F}$

Model	\hat{c} [1]	L [m]
Hydraulic radius (Walsh and Brace (1984))	1/2 (tube) 1/3 (crack)	$m = (V_p/A_p)$
Hg-Porosimetry (Katz and Thompson (1986) and (1987))	1/226	l_c
Tube-Crack (Guéguen and Dienes (1989))	1/8 (tube) 8/15 (crack)	r_A (tube) w_A (crack)

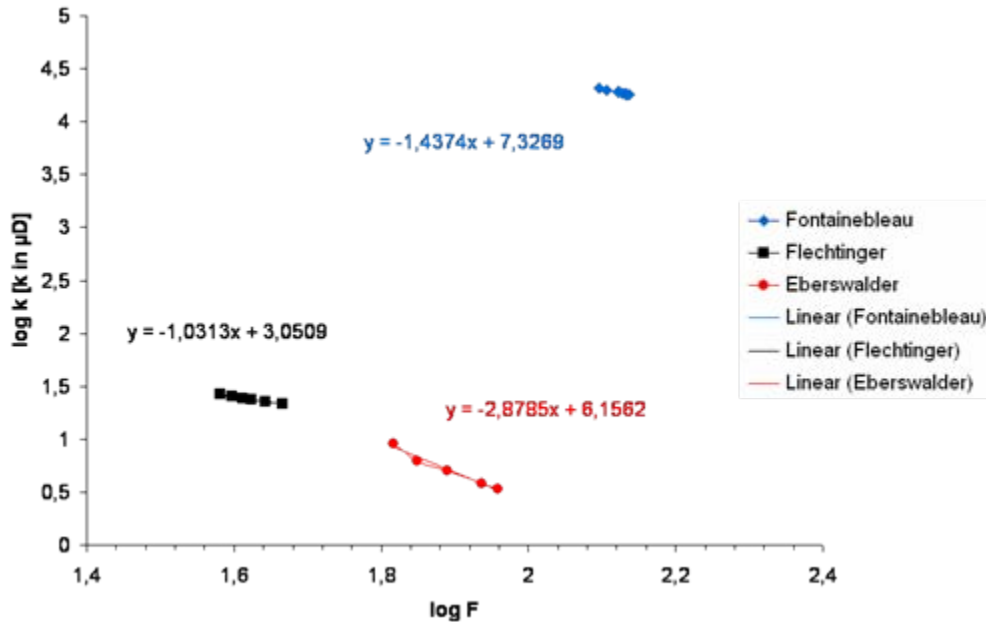
Comparison of different scaling models (cont.):



$$k = c \cdot L^2 \cdot \frac{1}{F}$$



Comparison of different scaling models (cont.):



$$\boxed{k = c \cdot L^2 \cdot \frac{1}{F}}$$

but

$$\boxed{k = c \cdot L^2 \cdot \frac{1}{F^r}}$$

- experiments yield **sample dependent** parameters

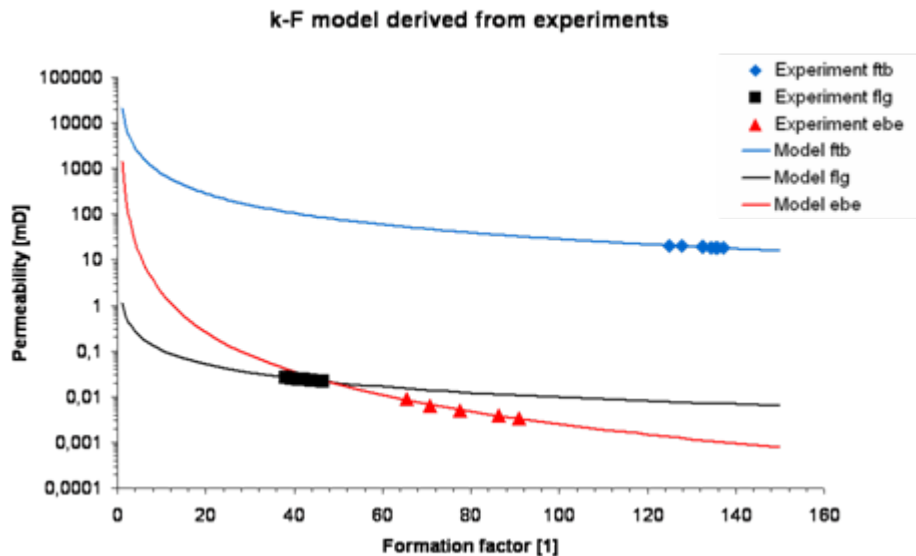
r and $(c \cdot L^2)$

- $(c \cdot L^2)$ is a **constant** defining the “permeability” of an equivalent tube-like channel for which $F = 1$

- c and L^2 cannot be derived separately from the experiments but have to be calculated from the model of choice

- L is thus a parameter with **no true microstructural meaning**

Comparison of different scaling models (cont.):



$$k = c \cdot L^2 \cdot \frac{1}{F^r}$$

Sample	r [1]	cL ² [mD]	L [μm] with c = 1/8
ftb	1.44	21.23 · 10 ³	13.03
flg	1.03	1.124	0.095
ebe	2.88	1.43 · 10 ³	3.38

6. Conclusions

- At present, the investigated models have to be adjusted for each rock by additional empirical parameters to reproduce the experimentally observed k-F relationship adequately.
- Potentially, an independent evaluation of k and F as a function of the (pressure dependent) sample microstructure could yield improved k-F relationships.
- Microstructure-based models require improved analytical methods.
- **All models have to be experimentally testable.**