

1 **New fault slip distribution for the 2010 M_w 7.2 El Mayor Cucapah**
2 **earthquake based on realistic 3D finite element inversions of coseismic**
3 **displacements using space geodetic data.**

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13 Key point #1:

14 El Mayor Cucapah fault slip distribution is optimized in a realistic numerical environment to
15 match geodetic data with minimal residuals.

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18 Key point #2: Optimization with material heterogeneities fits better the observed
19 deformation pattern with respect to the homogeneous case.

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22 Key Point #3: Numerical results find no shallow slip on the southernmost fault plane.
23

24 **Abstract**

25
26 In this work we investigate the 4 April, 2010, M_w 7.2 El Mayor-Cucapah (EMC) earthquake.
27 Existing studies modeled the EMC area as an elastic half-space in a homogeneous or vertically
28 layered structure, which, along with differences in data and inversion methodologies, led to
29 considerable variability in the resultant fault slip models. To investigate the EMC earthquake more
30 realistically, we first examine how published coseismic fault slip models have approached the
31 problem and what are their findings, then we select the optimal geometry and slip of one most
32 recent and comprehensive coseismic fault slip model, obtained through analytical inversions, and
33 adapt them in a three-dimensional finite element numerical environment where we assess the effects
34 of topography and material heterogeneities. Numerically optimized slip models are obtained via
35 joint inversion of GPS, interferometric synthetic aperture radar and subpixel offset datasets. We
36 find the effect of topography to be negligible while the inclusion of material heterogeneities
37 enhances the slip at depth, as might be expected where the medium has higher rigidity, and better
38 fits the displacements at both near and far field, especially around the Salton Sea area. The match
39 with geodetic data is significantly improved when the fault slip is increased at the fault planes close
40 to the epicenter and deeper at the southernmost plane, with respect to the slip of the chosen

41 analytical model. Our findings suggest that this earthquake was associated with a higher and more
42 spatially concentrated slip than previously thought implying a greater stress drop at depth.

43

44 **1. Introduction**

45

46 The 4 April 2010 El Mayor Cucapah (EMC) earthquake struck northeastern Baja California, near
47 the border between California and Mexico. This area is characterized by several transform faults
48 which accommodate the relative motion between the Pacific and North American plates, with the
49 former moving NW at a rate of ~48-52 mm/year (Argus et al., 2010; DeMets et al., 2010) with
50 respect to the latter. As pointed out by Fletcher et al. (2014), multifault ruptures in the area are the
51 result of different mechanisms including restraining bend tectonics, gravitational potential energy
52 gradients, three-dimensional strain of the transtensional and transpressional shear regimes. The
53 EMC epicenter was located at Long. $=-115.27^\circ$ and Lat. $=32.30^\circ$, according to the Southern
54 California Seismic Network (SCSN) catalog. With $M_w=7.2$ (<https://www.globalcmt.org>), this is one
55 of the larger seismic events ($M_w >6$) that has occurred in the area since 1987 (Spinler et al., 2015;
56 Gonzalez-Ortega et al., 2018). Its occurrence caused damage to roads, buildings and power lines in
57 the city of Mexicali, with extensive damage also reported throughout agricultural areas (Stenner et
58 al., 2010). A comprehensive report has been released by Meneses et al., 2010 (EERI Report No.
59 2010-02). The EMC earthquake is peculiar for two main reasons: 1) it was characterized by a
60 bidirectional rupture extending more than 120 km along strike and oriented NW-SE; 2) radar
61 interferometry, seismicity, field measurements and creepmeters (Hauksson et al., 2011; Fletcher et
62 al., 2014; Gonzalez-Ortega et al., 2014) reveal that this event activated more fault segments than
63 any other prior event in the area: Pescadores, Borrego, Paso Inferior, Paso Superior in the northwest
64 and the Indiviso to the southeast (rather than the expected seismogenic Cerro Prieto fault). To the
65 north in California, numerous faults were also involved: the San Andreas, Superstition Hills,
66 Imperial, Elmore Ranch, Wienert, Coyote Creek, Elsinore, Yuha and several minor faults near the
67 town of Ocotillo (Wei et al., 2011b; Kroll et al., 2013; Donnellan et al., 2014). Fault motion was
68 mainly right-lateral strike with some normal component. The EMC earthquake is also thought to be
69 responsible for increasing the gas flux of a series of mud volcanoes located near the Salton Sea
70 (Rudolph and Manga, 2010); in particular, these authors suggest that strains up to 1.2%, induced by
71 the earthquake near the mud volcano location, may have increased the permeability, which in turn
72 affected the volcano degassing activity. Trugman et al., (2014) observed that anthropogenic fluid
73 extraction at Cerro Prieto Geothermal Field site (at approximately 15 km NE of EMC epicenter)
74 may have contributed to destabilizing the area before the earthquake by generating positive
75 Coulomb stress rates on the order of 15 kPa/yr near the hypocenter and so exceeding the local

76 tectonic stressing rate. The main shock was followed by numerous aftershocks around the epicenter,
77 defining a seismogenic zone extending to a depth of about 10 km (Castro et al., 2011).

78

79 **1.1 Previous studies**

80

81 Several authors have studied this event through analytical and numerical inverse modeling of
82 different sets of data, such as teleseismic body waves, GPS, interferometric synthetic aperture radar
83 (InSAR) and subpixel offsets, in order to characterize the number of fault segments involved and
84 the fault slip distribution. Results show that measured geodetic data require assuming the existence
85 of a NW-SE oriented multi-segment fault system, with each segment having variable strike and dip
86 angles. Despite the detailed observations of the fault trace at the surface obtained from geological
87 (Fletcher et al., 2014) or differential LIDAR measurements (Oskin et al., 2012), there is no general
88 agreement on the number of fault segments actually involved. For example, Wei et al. (2011a)
89 performed joint inversions of geodetic, remote-sensing and seismological data using a simulated
90 annealing algorithm, obtaining the best match using a 4-segment fault geometry. Uchide et al.,
91 (2013) inverted strong motion data to infer the slip distribution on a 6-segment fault geometry,
92 while joint inversions of SAR, optical and GPS (continuous and campaign) data by Fialko et al.
93 (2010) suggested the presence of 7 fault segments. Finally, the analytical joint inversions of GPS,
94 InSAR and subpixel offset data by Huang et al. (2017, hereafter Huang17) indicated a geometry
95 composed of 9 fault segments (Fig. 1). Most of these studies were based on simplified assumptions
96 that underestimate the complexity of the area, often represented as a half space with no topography.
97 Moreover, no interaction is assumed to exist between adjacent fault planes and the medium is
98 treated as elastically homogeneous or, in some cases, as vertically stratified. These assumptions
99 might lead to biases in the estimation of the amount and distribution of slip at depth. Hauksson et al.
100 (2015) show for example that at depth, under the NW-SE fault rupture profile, there is a strong
101 variation of V_p and this suggests that accounting for full heterogeneities (vertical and lateral) may
102 be a viable way to better reproduce the correct response of the medium. In order to understand if the
103 existing assumptions are sufficient to describe the event or can rather jeopardize its interpretation,
104 we performed a 3D finite element model inverting GPS, InSAR and subpixel offset data from
105 Huang17, assessing the contribution of topography and full heterogeneities. In Section 2, we
106 describe the model. In Section 3, we present the data. In Section 4 we show the results. In Section 5,
107 we discuss our findings and provide conclusions.

108

109 **2. Model**

110

111 To study the EMC, we develop a finite element method (FEM) model and its solution using the
112 commercial software COMSOL Multiphysics v5.4. The model represents an area extending from
113 the northeast tip of the Gulf of California to the Mojave Desert (Fig. 1, inset). This extent allows us
114 to include a consistent number of GPS stations in both the US and Mexico, and to take into
115 consideration the area covered by the InSAR and optical observations as well. The area is
116 numerically represented by a 540x440 km 3D domain which extends to 150 km depth (Fig. 2a). The
117 main domain is framed by a set of domains that are further extended numerically using an “*infinite*
118 *element*” setting. The infinite element applies a real-valued coordinate scaling (or stretching) to the
119 domains surrounding the physical region of interest and having coincident nodes. The domains are
120 scaled by default to be very much larger than the original geometry and the finite distance to the far-
121 away boundary allows prescribing standard boundary conditions. By stretching the domains, we
122 avoid possible boundary effects which could arise from a premature truncation. Into the main
123 domain, the fault system (Fig.1) is embedded following the geometry suggested by Huang17. The
124 fault system consists of 9 shell-type fault planes with different strike and dip angles and a maximum
125 depth of 16 km below the top surface (Fig. 2a). Embedding the fault planes into a continuum
126 domain overcomes the need of building complex twisted noncoplanar connecting surfaces, still
127 assuring the interaction between adjacent planes and the continuity of the displacement field
128 without forcing *a priori* geometrical connections between the different fault segments. Topography
129 is included using a digital elevation model (DEM) from the Shuttle Radar Topography Mission
130 (SRTM) data with 30 m resolution (<https://www2.jpl.nasa.gov/srtm/>). In particular, DEM data are
131 imported and included in the model in the form of a “*parametric surface*”, where the parameter is
132 the DEM elevation mapped to a series of points on the domain top surface, generating a realistic
133 topography (Fig. 2b). No bathymetry is used. In terms of material properties, the medium can be
134 treated as elastically homogeneous or with vertical heterogeneities (layered) or with vertical plus
135 lateral heterogeneities (hereafter, heterogeneous). For the first two cases, we adopt the same
136 parameters given by Huang17 in their table S2. The layered case considers a vertically variable
137 Young’s modulus (Fig. 2b) and a constant Poisson’s ratio of 0.25 while full heterogeneities (Fig. 2c,
138 2d) are obtained using the V_p , V_s and density data from the SCEC Community Velocity Model
139 Harvard v15.1.1 (<https://scec.usc.edu/scecpedia/CVM-H>) and converting them into elastic moduli
140 using the Christensen and Mooney (1995) empirical law. Material parameters are summarized in
141 Table 1. Because the model is kinematic, density is not relevant. The mesh for the domain volumes
142 is composed of tetrahedral elements while the outside boundaries are discretized using triangular
143 elements. At the top surface, the mesh is finer in proximity of the fault trace and becomes coarser

144 away from the area of interest (Fig. 3a). Fault planes along the fault trace are discretized into 432
145 patches using quadrilateral elements of about 2x2 km, in order to have a regular mesh and better
146 control on the fault slip distribution, while triangular elements are used for the transverse plane to
147 better control its intersection with one of the planes along the fault trace (Fig. 3b). We assign 1 m
148 slip to each fault plane and perform direct mesh sensitivity tests in order to find a reasonable
149 balance between the mesh quality and a solution which does not change with further refinements.
150 The domain top surface is stress-free while the bottom is fixed. A roller condition (no displacement
151 in the normal direction) is applied at the side boundaries. Fault segments are treated with the so
152 called “*thin elastic layer*” condition and a prescribed slip (right-lateral and dip-slip components, as
153 suggested by Huang17). The thin elastic layer condition allows having two sets of coincident mesh
154 nodes for the two sides of the shell. We perform a joint optimization of GPS, optical and InSAR
155 data using the gradient based optimization algorithm SNOPT (Gill et al., 2005), available in
156 COMSOL. Details about SNOPT are given in paragraph S2 of the Supporting Information.

157

158 **3. Input Data**

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160 Recorded geodetic data are taken from Huang17 (see their supplementary material). In particular,
161 three sets of geodetic data are used in our model: GPS, InSAR and subpixel offsets
162 (<https://doi.org/10.5281/zenodo.4290782>). GPS data consist of 23 near field stations installed on the
163 Mexican side by the researchers of the Centro de Investigación Científica y de Educación Superior
164 de Ensenada (CICESE) a few days after the event and 132 near to far field PBO stations from the
165 UNAVCO Data Center, located on the US side. InSAR data consist of a total of 4433 down-
166 sampled points from ascending and descending tracks of ALOS PALSAR and ENVISAT ASAR
167 SAR sensors. For each point, Huang17 provided longitude, latitude, azimuth, view-angle and value
168 along the satellite line-of-sight (LOS). We convert azimuth and view angle into the three direction
169 cosines, in order to project the model top surface displacements into the LOS. Subpixel offset data
170 include SPOT5 satellite optical image pair for the E-W and N-S components at 293 points. Starting
171 from the geometry and slip reported in Huang17 (see their Supplementary Material Table S1), we
172 first validate the FEM model by checking that the numerical output at selected GPS stations is
173 consistent with the output obtained analytically, using Okada (1985) type dislocations (see
174 Supplementary material Fig. S1). Once the model has been validated, we assess if, for the same slip
175 distribution, the model predictions at the GPS sites show a good fit compared to the recorded
176 coseismic displacements. The results show that the vectors obtained using the slip from Huang17 do
177 not fit perfectly with the measurements (Fig. 4a). In particular, while globally the two solutions

178 show vectors with similar orientation (except for a few stations), the vectors obtained using the slip
179 from Huang17, underestimate (up to 40%) the measurements in both horizontal and vertical
180 components at almost all stations (Fig. 4b). Therefore, with our numerical approach, we use
181 Huang17 slip distribution solution as an initial guess to guide the model and then perform a joint
182 inversion in the more realistic FEM computational environment. The goal is to find a new slip
183 distribution whose output better fits the observations. Details on the inversion methodology are
184 provided in paragraph 2 of the supplementary material.

185

186 **4 Results**

187

188 In this section, we compare the output at the model top surface, obtained from our joint
189 optimization, to the recorded GPS, InSAR and subpixel offset datasets. Residuals and standard
190 deviation are also calculated for all cases (Table 2) and compared to the one obtained from the
191 Huang17 solution.

192

193 **4.1 Comparison with GPS data**

194

195 Figure 5a and 5b show the comparison between the predicted (numerically optimized) solution and
196 the observed surface displacements for the homogeneous case. For visualization purposes, the
197 comparison is restricted to the near field GPS stations east of the fault trace, which are the ones
198 showing significant horizontal displacements of several centimeters. These include 17 Mexican
199 stations and 4 PBO stations. Comparing Figures 5a and 5b with Figures 4a and 4b, we see that the
200 optimized slip solution produces predicted displacements in better agreement with the observations.
201 Error ellipses are not shown because the associated error for the GPS stations is about 4 mm and
202 won't be visible at the chosen scale. Slight misalignments appear at BG51 and VM15 stations. This
203 appears to be an effect of the joint inversion, since the model must fit with a reasonable balance
204 three sets of data. Not surprisingly, when we invert for the GPS data only (see Supplementary
205 Material figure S3) a better fit is obtained at these stations.

206 Next, we examine the effects of layered and heterogeneous structure. Figure 6a extends the results
207 of Figure 5a including the displacement vectors obtained from the joint inversion for the layered
208 and heterogeneous case. All solutions have a coherent SE pattern with respect to the recorded data,
209 which is consistent with the expected direction of displacement on the eastern side of the fault
210 (since the slip is right-lateral strike). The vectors belonging to the homogenous solution being
211 slightly bigger (about 1 cm) than the layered and heterogeneous solutions, as can be seen in their
212 difference vectors (Fig. 6b). A similar discrepancy (1-2 cm) between the length of the vectors of the

213 homogeneous solution versus the ones for the layered and heterogeneous can also be observed in
214 the far field in the area around the Salton Sea (Fig.7a). In both cases, (near and far field) we see that
215 the homogeneous solution vectors over-predict the observed displacements. This result is in line
216 with the geology of the area. As shown in Rollins et al., (2015) (see their Fig 1a), the area near the
217 Salton Sea belongs to the Salton Through, a region featuring a shallow lithosphere–asthenosphere
218 boundary and shallow Moho and distinct from the surrounding area of the Peninsular Ranges. Our
219 solutions (layered and heterogeneous) are able to capture these differences giving vectors closer to
220 the measurements, while the use of a homogeneous domain would produce a systematic misfit.
221 However, since the layered and heterogeneous solutions produce very similar vectors (blue and gray
222 vectors almost overlap), we can conclude that the differences described above are mostly driven by
223 the vertical heterogeneities rather than the horizontal ones. Vertical components are captured
224 almost equally showing an uplift south of the Salton Sea, as expected. Comparisons between the
225 Huang17 solution and our solution for all GPS stations in terms of standard deviation (Table 2)
226 shows that numerical joint optimization improves the total standard deviation by about 50%.

227

228 **4.2 Comparison with InSAR data**

229

230 Referring to the same area as in Figure 1, Figure 8 shows the measured, modeled and residual
231 (measured-modeled) results for the InSAR ascending and descending tracks in the homogenous
232 case. The comparison shows that the homogeneous joint inversion fits well with the recorded data
233 so that residuals are close to zero. The difference (residuals) between predictions of models
234 assuming homogeneous and layered structure (H-L) or homogeneous and heterogeneous structure
235 (H-He) for the ascending and descending tracks are shown in Figure 9. For both cases, the inclusion
236 of heterogeneities implies changes in the range of ± 0.05 m. The H-He case produces slightly larger
237 residual values with respect to the H-L case, which means that, as found for the GPS data, that the
238 output obtained for the heterogeneous case is lower in magnitude than the layered one.
239 Quantifications in terms of standard deviation for all material configurations are shown in Table 3.
240 Numerical optimization improves the standard deviation of InSAR data by 45% for the ascending
241 track and by 22 % for the descending track with respect to Huang17 solution.

242

243 **4.3 Comparison with subpixel offset data**

244

245 Referring to the same area as in Figure 1, Figure 10 shows the measured, modeled and residual
246 results for the subpixel offset datasets EW component (top row) and NS component (bottom row) in

247 the homogenous case. When we look at the residual for the EW component, most points drop to
248 about zero values, however we can also notice that some of them in the very north and central part
249 of the fault shows values in the range ± 0.5 m. Residuals for the NS component appear instead more
250 uniform with values between 0 and -0.3 m. Figure 11 shows the residuals of the H-L and H-He
251 model predictions, the latter giving slightly higher values. Globally, residuals from the FEM
252 solutions are in the range of ± 0.05 m for the EW component and ± 0.10 m for the NS component.
253 Quantifications in terms of standard deviation for all material configurations are shown in Table 4.
254 Numerical optimization improves the total standard deviation by 10% with respect to the analytical
255 solution.

256

257 **4.4 Non optimized vs optimized slip distribution**

258

259 Figure 12 shows the slip distribution on the fault planes. The not optimized slip (Fig.12a) which
260 corresponds to the solution from Huang17, is compared to the optimized slip in the homogeneous,
261 layered and heterogeneous domains (Fig. 12b, 12c and 12d, respectively). Qualitatively we can
262 observe that, as a result of the optimization, the slip is increased in all planes. For a better
263 understanding we assign a number to each plane with the leftmost plane being the plane number 1
264 and rightmost the plane number 8. The 40° E transverse plane is number 9. The increase with
265 respect to the starting solution is clearly observed at the top part of plane 2 (in correspondence to
266 the Borrego fault), at planes 4 and 5 (in correspondence to the Pescadores fault), at the top right part
267 of plane 6 and at plane 8 (Indiviso fault). Moreover, the slip on plane 8 is centered at about 8 km
268 depth in our FE optimized joint solution, which is deeper than the solution found through analytical
269 joint inversions by Huang17, where the slip appears to be centered at above 5 km depth. Slip on
270 plane 9 is shown only for the Huang17 solution, because it is similar for all cases. In particular,
271 about 1 m, quite uniform slip is found on this plane, which is consistent with an unfavorably
272 oriented fault with respect to the regional stress field, as pointed out by Fletcher et al. (2016). The
273 layered and heterogeneous solution (Figure 12c and 12d) shows higher slip at depth (especially on
274 plane 6) with respect to the homogeneous case (Figure 12b). This is consistent with the higher
275 rigidity of the medium at depth combined with the plane position and dip angle. The vertically
276 stratified (layered) and the 3D heterogeneous models however have a more similar slip distribution.
277 Figure 13 helps to quantify the differences between the different cases. Figure 13a shows the
278 residual between the slip distribution before (Huang17) and after the optimization in the
279 homogeneous domain. We can observe an increase of the slip by up to 3 meters and that the slip
280 distribution is more compact on planes 2, 4 and 8 while all of plane 5 is required to slip. Figure 13b

281 shows the residual between the layered and the homogeneous numerical solutions. An increase of 1-
282 2 meters is observed at depth on plane 6 while in some areas the increase is between 0.5 and 1 m.
283 These last however, appear to be too sporadic to infer a uniform slip and we think that they are a
284 combined effect of the material properties and the plane's dip angle. Figure 13c shows the residual
285 between the heterogeneous and the homogeneous cases. Because the slip for the layered and
286 heterogeneous solutions are similar Figure 13c is similar to Figure 13b, and in turn the residual
287 between the slip distributions for the layered and the heterogeneous cases (Fig 13d) are very similar,
288 with minor differences in the ± 1 m range.

289 Our tests indicate that when we start from Huang17 joint slip solution and perform the numerical
290 inversions, the slip on plane 8 becomes greater and deeper when InSAR data are included in the
291 joint inversion, while it remains unchanged (same as starting solution) if the inversion is performed
292 considering the GPS data only (see figure S4 in Supplementary Material). We would expect a
293 similar finding from Huang17 during the inversion of the InSAR data (which are the only data
294 available in that area) instead, in their Figure 4, the authors show that a slip higher than 5 m appears
295 on the southernmost plane when subpixel offset data (only) are inverted while, in the inversion for
296 InSAR data only, their slip on plane 8 looks deeper and having a value of about 2 m. This means
297 that, in their joint solution, the strong slip on plane 8 is driven by the subpixel offset data, however
298 because these data are obtained combining InSAR and Optical datasets, with the latter being only to
299 the north of the epicenter, there are no subpixel offset data to the south and, therefore, it is more
300 reasonable to find slip on that plane when InSAR data are considered, as in our case. In order to
301 understand the effect of the initial guess on the slip distribution of plane 8 in the joint numerical
302 solution, we performed an additional test keeping the solution from Huang17 as the initial guess in
303 all planes except plane 8, where we assume instead a uniform slip of 1 m on plane 8 at the
304 beginning of the optimization. When we do so, the model finds again a slip similar to the one we
305 obtain using the Huang17 solution as the starting guess. This time its value is smaller (about 5 m)
306 and also has a shallower appendix on top (Fig.14). We will call this solution intermediate slip,
307 where intermediate is to be intended as intermediate depth to discriminate from the deeper one.
308 Even though it's hard to have high level confidence about the slip distribution at depth on this plane
309 (because the inversion depends only on few pixels of the InSAR dataset), our checkerboard tests
310 (see Supplementary material Figures S2) prove that our model is capable to reasonably resolve a
311 predefined slip distribution when inverting for the top surface data (even perturbed) so we can
312 exclude the effect of numerical artefacts in the solution. The results obtained for both cases suggest
313 that a very shallow slip (close to the fault trace) is unlikely to occur and this is in line with what was
314 observed in the field in this area, where the fault trace appears sporadic (Fletcher et al., 2014). To

315 see which solution (deep or intermediate) would be more in line with existing data, we cross-
316 checked the output of the two solutions at the GPS stations located at the western side of the fault
317 trace, which are mostly affected by the northwestward motion of the fault. Figure 15 shows that the
318 solution with the deeper and strong slip (red vectors) and the one with intermediate and weaker slip
319 (blue vectors) are similar. This is because, in both cases, the model has to fit the recorded data, so
320 that in the intermediate slip case, the value is smaller than the deeper solution. A comparison at
321 SALD (which is the station closest to the plane) shows that the intermediate slip produces a vector
322 whose orientation is slightly closer to the observation. The solutions with a deeper or intermediate
323 slip on the southernmost plane are also compared in terms of residuals with the recorded data for
324 the InSAR (Fig.16). We can observe that in the intermediate slip case, a slightly lower residual is
325 visible near the SE tip of the fault trace. No comparison is necessary with the subpixel offset data,
326 because there are no subpixel offset data near plane 8. Independent calculations, as the one
327 performed by Fialko et al. (2010) or Kyriakopoulos et al. (2017) (preferred model) also exclude
328 very shallow slip on plane 8. This agreement is noteworthy because greater slip at depth is
329 important for postseismic afterslip and relaxation analyses and may also have implications for
330 dynamic fault models and aftershock generation. Finally, to understand if our slip distribution is
331 reasonable, we calculated the seismic moment and the corresponding moment magnitude M_w using
332 the following formula:

333

$$334 \quad M_0 = \mu * D * A \quad (1)$$

$$335 \quad M_w = \frac{2}{3}(\text{Log}(M_0) - 6.04) \quad (2)$$

336

337 where μ is the shear modulus, D the slip and A the fault plane area. We obtain the results shown in
338 Table 5, with a moment magnitude close to the GCMT value.

339

340 **5. Discussion and Conclusions**

341

342 In this work we investigate the coseismic displacements of the El Mayor Cucapah earthquake.
343 Because of the complexity of this event, related to the number, location and kinematics of the
344 activated fault segments, several interpretations of the slip distribution (obtained from the inversion
345 of different geodetic datasets) exist. Prior studies show that the variability of the interpretation
346 depends on the data sets used and the underlying assumptions, such as the use of a flat stress-free
347 surface, instead of a realistic topographic relief, and/or a simplified characterization of the real
348 material properties. We choose one of the most complete published results, obtained through

349 analytical inversions by Huang17, as a starting point (same fault planes configuration and same
350 reported slip) for our model and use the capability of the numerical (finite element) approach to test
351 the goodness of the corresponding output when adding additional complexity (e.g. the presence of
352 topography) and further optimizing the slip distribution using different material configurations. We
353 first perform a series of direct tests. Our direct tests show that the numerical model can reproduce
354 the output obtained analytically for a dislocation in a halfspace, so no artificial numerical effects
355 exist due to the chosen geometry and level of discretization (mesh). When topography is used, the
356 numerical output produces minor changes (less than 2%) with respect to the flat case, a result which
357 is consistent with the low topographic relief of the area and is in line with other independent
358 analyses (Kyriakopoulos et al., 2017). The effects of topography are found to be small even in
359 cases where topographic variations are substantial (e.g., Wang and Fialko, 2018). For this reason,
360 topography is neglected in the subsequent analyses. The use of the Huang17 solution in a direct
361 numerical model generates near field GPS displacement vectors which underestimate the observed
362 data.

363 To improve the fit in the near field and take into consideration the data in the far field, we start from
364 the solution of Huang17 as an initial guess to guide the model, and use all the available geodetic
365 datasets (GPS, InSAR and subpixel offset) to perform joint numerical inversions, taking into
366 account the contribution from different material configurations (including vertical and vertical plus
367 lateral heterogeneities). Preliminary checkerboard tests prove that the method used for the inversion
368 is reasonably robust. Results of our finite element joint inversions show that higher slip is required
369 on the central planes near the epicenter, with respect to the slip distribution reported by Huang17, to
370 get a good match with recorded GPS data. A good fit is also found against the InSAR and subpixel
371 offset data, with minimal residuals. The comparison between the different surface displacements
372 obtained from the homogeneous, layered and heterogeneous material configurations shows that all
373 solutions have a coherent pattern and that using a homogeneous material gives greater
374 displacements, with the layered being intermediate in magnitude and the heterogeneous being the
375 smallest. Since the heterogeneous case is the most realistic case, this means that limiting the
376 analysis to a homogeneous or layered material (as in most of the analytical approaches) may
377 introduce a systematic misfit in the estimation of the computed surface displacements, while with
378 the numerical approach we are able to detect and overcome this limitation and better fit the
379 observed displacements. This is particularly evident when we look at the displacement vectors in
380 the Salton Trough area where the solution corresponding to the inversion performed with a layered
381 or heterogeneous model captures better the displacement field with respect to the homogeneous
382 case. Compared to other models, our slip distribution has similarities but also differences. Similar to

383 Fialko et al., (2010), Wei et al. (2011) Kyriakopoulos et al. (2017) and Huang et al. (2017) most of
384 the slip is found near the epicenter (Pescadores Fault) and at the end of the Indiviso fault. However,
385 in the preferred model of Kyriakopoulos et al. (2017), the slip from the Pescadores Fault to the
386 Borrego Fault does not show any interruption while we are able, instead, to find a good
387 correspondence with areas having low or no slip like the PIAZ and PAZ accommodation zones
388 (Figures 1 and 12). Our joint inversions also show a greater and deeper slip at the southernmost
389 plane, with respect to the starting solution of Huang17. However, since the Huang17 solution on
390 plane 8 seems to be driven mostly by subpixel offsets rather than InSAR, we performed one
391 additional test without using Huang17 as the starting solution on this plane. Results confirm that
392 when we start from a 1 m uniform slip, a deeper slip still appears as an effect of the InSAR data,
393 which means that the result is somehow consistent with our previous finding. However, in this
394 second case, the slip is slightly more extended (with a shallower part) and smaller than the
395 numerical solution obtained using Huang17 as the initial guess. To check which of the two
396 solutions (intermediate or deep) is preferred, we test the outputs of both solutions on the GPS
397 stations located west of the fault trace, which are the ones mostly affected by the three westward
398 dipping planes (southward of the epicenter) and we compare these outputs to the measured data.
399 The GPS vectors on SALD, which is the station closest to the southernmost fault plane are in favor
400 of the solution with the intermediate slip. A slightly better agreement is also found with InSAR data
401 when the solution with the intermediate slip is chosen. In both cases, a very shallow slip is
402 excluded. Two aspects which may support the absence of a very shallow slip are the absence of a
403 clear fault trace in that area (which would be expected if the slip is close to the surface) and the
404 correspondence to other studies, which also found the slip to be deeper (Fialko et al. 2010,
405 Kyriakopoulos et al. 2017). Finally, our slip values and distributions are consistent with the
406 expected moment magnitude and close to the GCMT solution (max difference is about 2%) which
407 means that the slip distributions we found are also quantitatively reasonable. Because we use the
408 same fault geometries as Huang17 but we obtain a different slip distribution with our FEM
409 optimization, even when using the same homogeneous material properties, we can exclude that the
410 difference between their and our slip distribution is due to differences in the fault position and/or
411 orientation or in a different response of the medium and we speculate that instead the differences
412 between our slip distribution and theirs may be due to differences in their inverse method with
413 respect to ours. In particular, the use of an optimization algorithm tailored for a numerical
414 environment, rather than an analytical one, may be the cause of the improved fit to the recorded
415 data and the high confidence we obtain, which can provide new clues to better understand the
416 dynamics of such a complex event.

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421 link: <https://doi.org/10.5281/zenodo.4290782> .

422 The SCEC community velocity model is available at the website:
423 <https://scec.usc.edu/scecpedia/CVM-H>. The topography data are available at the website:
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434

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524

525 Captions

526 **Fig 1.** Map of the epicentral region of the El Mayor-Cucapah earthquake. Black dashed fault plane outlines represent
527 the geometry from Huang17. Red line represents the actual fault trace while the positions of the actual fault segments
528 are reported in blue. Red star is the epicenter location based on the Southern California Seismic Network (SCSN)
529 catalog. Beach ball is the focal mechanism is from Zheng et al., 2012. In the inset, the tectonic overview of Southern
530 California and Baja California including the Pacific–North America plate boundary and the California, Arizona and
531 Mexico borders. The red dashed box corresponds to the main figure.

532 **Fig 2.** a) Model geometry. The main domain is represented by a volume of 540x440x150 km, surrounded by a frame of
533 5 km thick domains with infinite elements. A 9-segment fault system is embedded into it. b) Layered configuration
534 with four different layers. Color scale represents the values of Young’s modulus (GPa). Model topography is also
535 shown at the model top surface. c) Young’s modulus (GPa) in a heterogeneous configuration. d) Poisson’s ratio in a
536 heterogeneous configuration.

537 **Fig 3.** a) Model mesh. The model volume is discretized with tetrahedral elements while triangular elements are used for
538 the surfaces. The inset at the bottom right corner shows the mesh near the fault trace. b) Inside view of the model

539 mesh showing the discretization on the fault segments. Eight NW-SE aligned fault segments are discretized using
540 quadrilateral elements while triangular elements are used for the transversal one.

541 **Figure 4.** a) Comparison between the GPS horizontal (vectors) and vertical (circles with associated color scale)
542 displacement components obtained using Huang17 solution (red vectors and inner circles) vs measurements (black
543 vectors and outer circles). Black line represents the fault trace. b) Huang17 solution horizontal displacement (black
544 solid line) and vertical displacement (black dashed line) versus measured horizontal displacement (red solid line) and
545 measured vertical displacement (red dashed line).

546 **Figure 5.** a) Comparison between the GPS horizontal (vectors) and vertical (circles with associated color scale)
547 displacement components for the optimized solution in the homogenous case (red vectors inner circles) and the
548 measured data (black vectors, outer circles). Black line represents the fault trace. b) Optimized solution horizontal
549 displacement (black solid line) and vertical displacement (black dashed line) versus measured horizontal
550 displacement (red solid line) and measured vertical displacement (red dashed line).

551 **Figure 6.** a) Horizontal (vectors) and vertical (circles with associated color scale) GPS displacement components.
552 Recorded (black), optimized homogeneous (red), optimized layered (blue), optimized heterogeneous (gray). The
553 outermost to innermost circle follow the order of the legend from top to bottom. Black line represents the fault trace.
554 b) Residuals of the horizontal and vertical homogeneous minus layered solutions (black vectors outer circles) and
555 homogeneous minus heterogeneous solutions (red vectors inner circles).

556 **Figure 7.** a) Horizontal (vectors) and vertical (circles) GPS displacement components. Dashed white line
557 represents the northern border of Salton Trough area. Recorded (black), optimized homogeneous (red),
558 optimized layered (blue), optimized heterogeneous (gray). The outermost to innermost circle follow the order of
559 the legend from top to bottom. b) Residuals of homogeneous minus layered (black vectors, outer circle) and
560 homogeneous minus heterogeneous solutions (red vectors, inner circle).

561 **Figure 8.** Measured (a,d), modeled homogeneous (b,e) and residuals (c,f) output for the InSAR data, ascending (top
562 row) and descending (bottom row) tracks. Black line represents the fault trace.

563 **Figure 9.** Residuals from the numerical solutions. a) ascending homogeneous-layered; b) ascending homogeneous -
564 heterogeneous; c) descending homogeneous-layered; d) descending homogeneous- heterogeneous. Black line
565 represents the fault trace.

566 **Figure 10.** Measured (a,d), modeled homogeneous (b,e) and residuals (c,f) output for the subpixel offset data EW (top
567 row) and NS (bottom row) components. Black line represents the fault trace.

568 **Figure 11.** Residual from the numerical solutions for the subpixel offset data. a) homogeneous-layered EW component;
569 b) homogeneous-heterogeneous EW component; c) homogeneous-layered NS component; d) homogeneous-
570 heterogeneous NS component. Black line represents the fault trace.

571 **Figure 12.** Slip distributions. a) Huang17 solution with plane 9 in the inset; b) Optimized solution in the homogeneous
572 case; c) Optimized solution in the layered case; d) Optimized solution in the heterogeneous case). Inset is excluded
573 from b, c and d as it is the same of a. Actual fault names and positions are shown in blue.

574 **Figure 13.** Residuals of the slip distribution from the different cases of the joint inversion. a) Homogeneous-Huang17
575 solution. b) Layered-Homogeneous. c) Heterogeneous-Homogeneous. d) Layered-Heterogeneous.

576 **Figure 14.** Optimized slip distribution in a homogeneous domain obtained using Huang17 solution as starting slip in all
577 planes except plane 8, where one meter uniform starting slip is applied.

578 **Figure 15.** Comparison between the horizontal (vectors) and vertical (circles) displacements at the western GPS
579 stations obtained from the measured data (black vectors) and the optimized solution with deeper slip (red vectors) and
580 intermediate slip (blue vectors) on the southernmost plane. The outermost to innermost circle follow the order of the
581 legend from top to bottom. Red dashed rectangle represents the position of the southernmost plane.

582 **Figure 16.** Residuals between measurements and the homogeneous joint inversion for the InSAR data with deeper (a, c)
583 and intermediate slip (b, d) on plane 8 for the ascending (top row) and descending (bottom row) tracks.

Tables

Table 1. Model material parameters in the homogeneous, layered and fully heterogeneous cases.

Homogeneous Model	Depth (km)	Shear modulus (GPa)	Poisson's ratio
	0-150	24.3	0.25
Layered Model	Depth (km)	Shear modulus (GPa)	Poisson's ratio
	0 - 5.5	24.3	0.25
	5.5 - 16.0	35.4	
	16.0 - 32.0	41.9	
	32.0 - 150	60.7	
Heterogeneous Model	Depth (km)	Shear modulus (GPa)	Poisson's ratio
	0 - 150	24 - 72	0.25-0.32

Table 2. Total, horizontal and vertical standard deviations for the analytical and numerical solutions (optimized) at the selected GPS stations.

Solution	σ_{tot}	$\sigma_{horizontal}$	$\sigma_{vertical}$
Huang17	0.112	0.108	0.123
FEM Homogeneous	0.057	0.048	0.074
FEM Layered	0.057	0.050	0.070
FEM Heterogeneous	0.058	0.052	0.070

Table 3. Total standard deviations for the analytical (homogeneous case) and numerical solutions (optimized) for the InSAR ascending and descending tracks.

InSAR Ascending Track	σ_{tot}	InSAR Descending Track	σ_{tot}
Huang17	0.128	Huang17	0.060
FEM Homogeneous	0.070	FEM Homogeneous	0.047
FEM Layered	0.072	FEM Layered	0.047
FEM Heterogeneous	0.072	FEM Heterogeneous	0.048

Table 4. Total, EW and NS standard deviations for the analytical (homogeneous case) and numerical solutions (optimized) for the subpixel offset dataset.

Subpixel offset solution	σ_{tot}	σ_{E-W}	σ_{N-S}
Huang17	0.327	0.392	0.246
FEM Homogeneous	0.293	0.329	0.254
FEM Layered	0.290	0.322	0.255
FEM Heterogeneous	0.290	0.321	0.255

Table 5. Moment magnitude from the not optimized (Huang et al. 2017), the optimized (FEM) and the Southern California Seismic Network Solution.

Material configuration	M_w Huang17	M_w FEM	GCMT
Homogeneous	7.26	7.24	7.20
Layered	7.32	7.33	
Heterogeneous	N/A	7.36	

Figure 1.

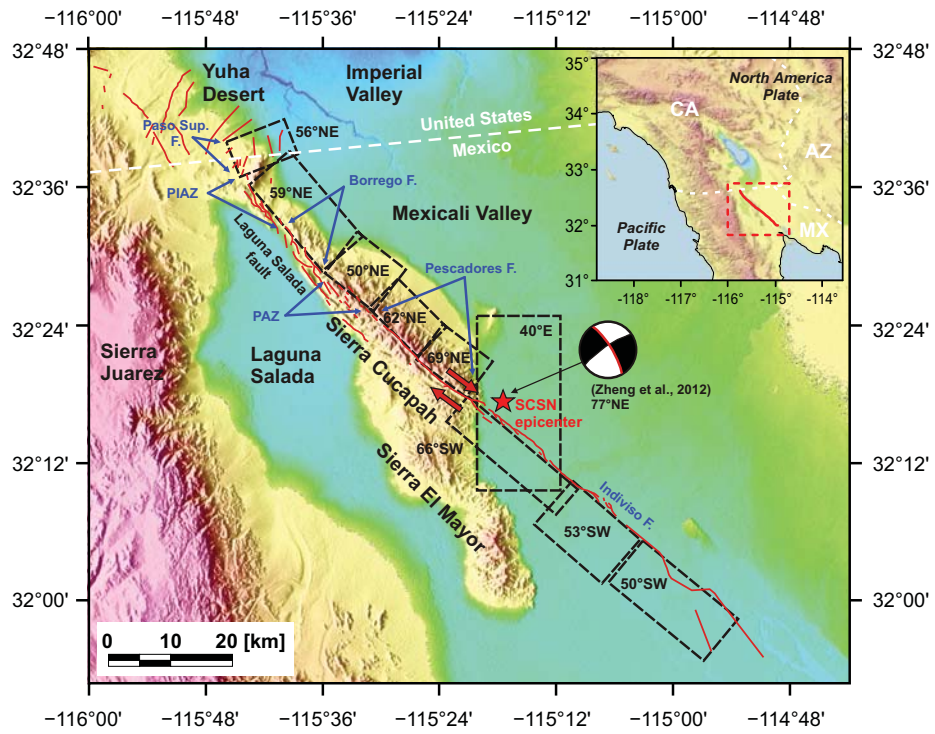


Figure 2.

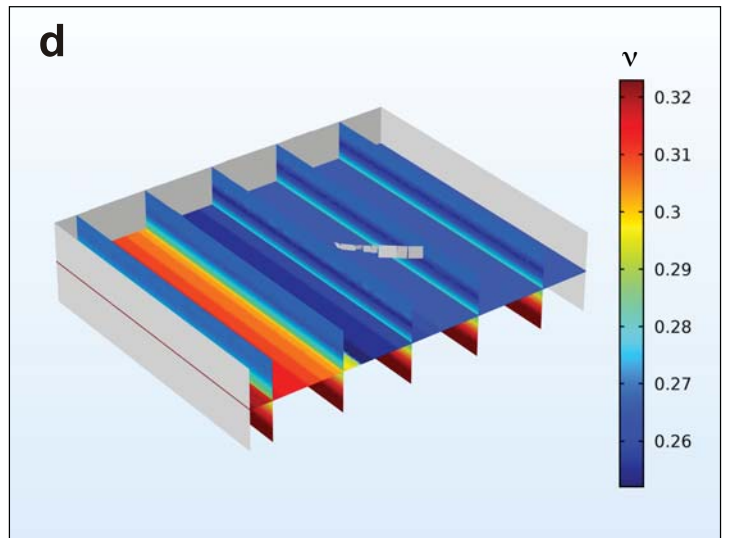
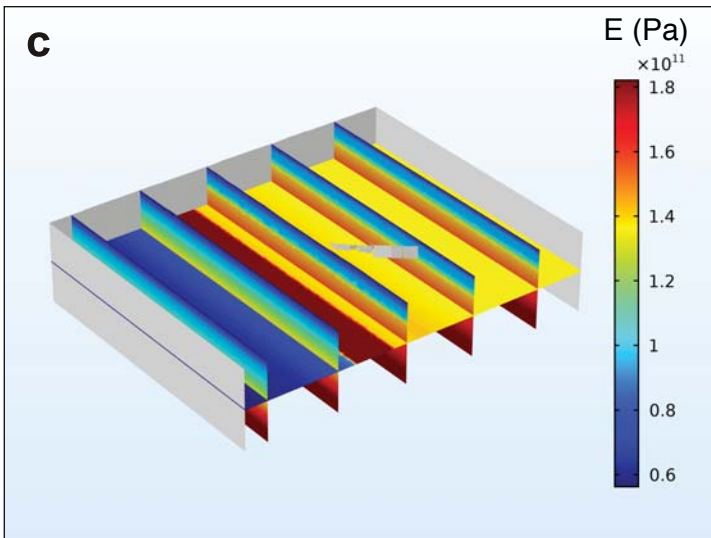
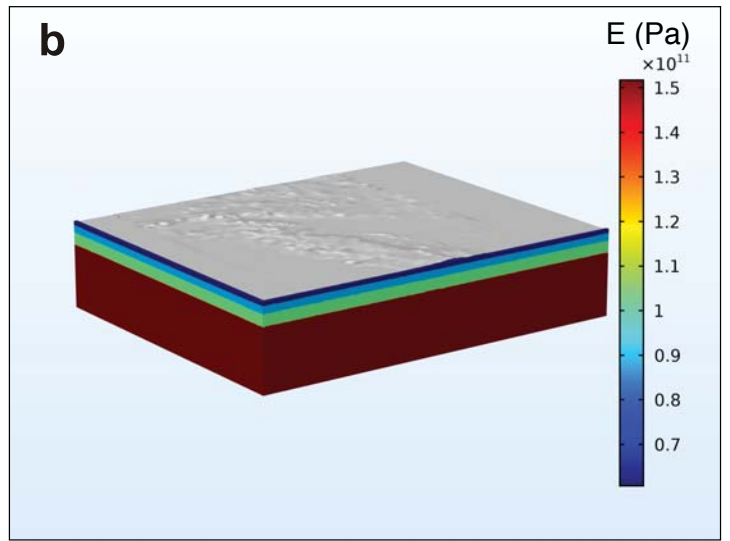
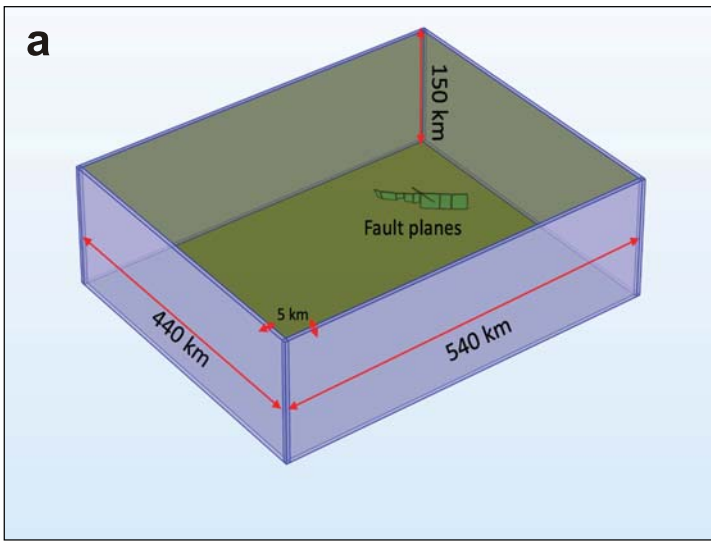
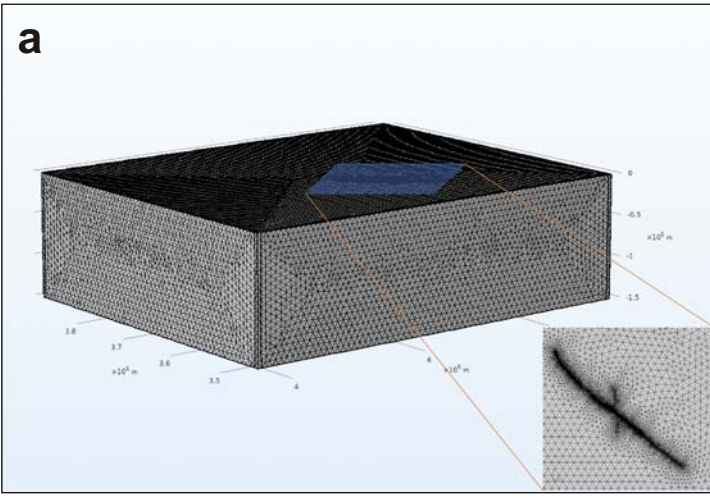


Figure 3.

a



b

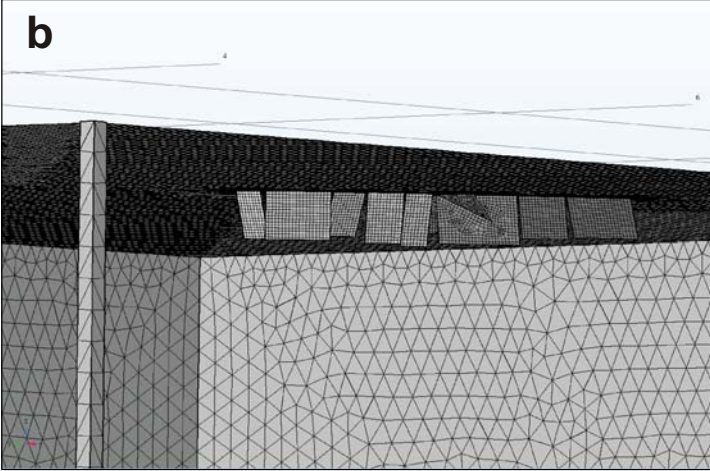


Figure 4.

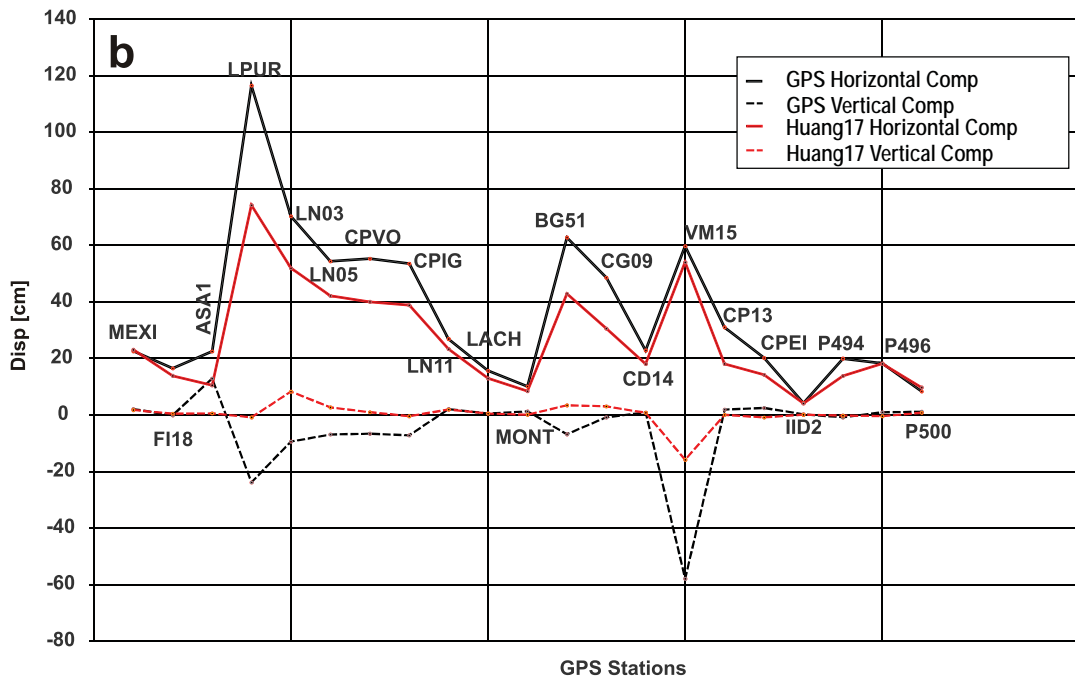
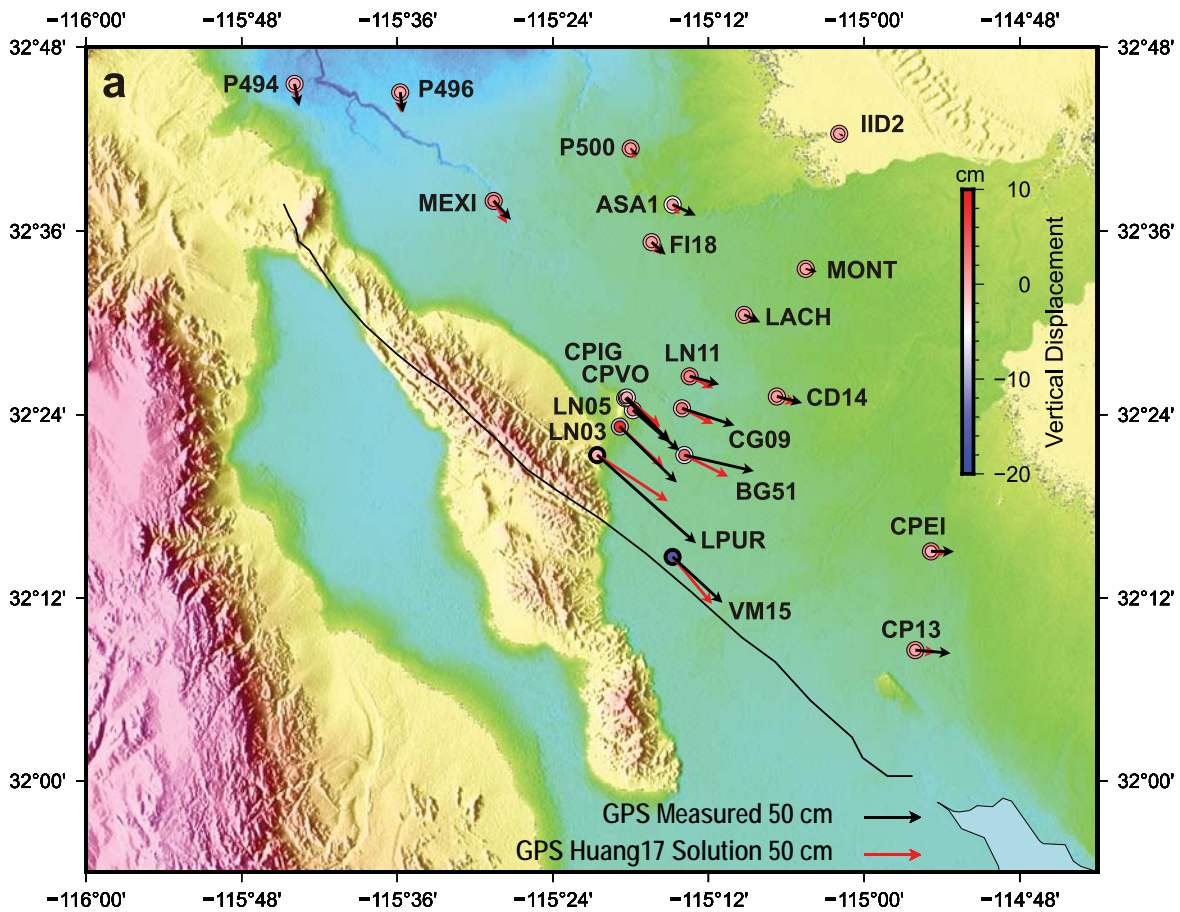


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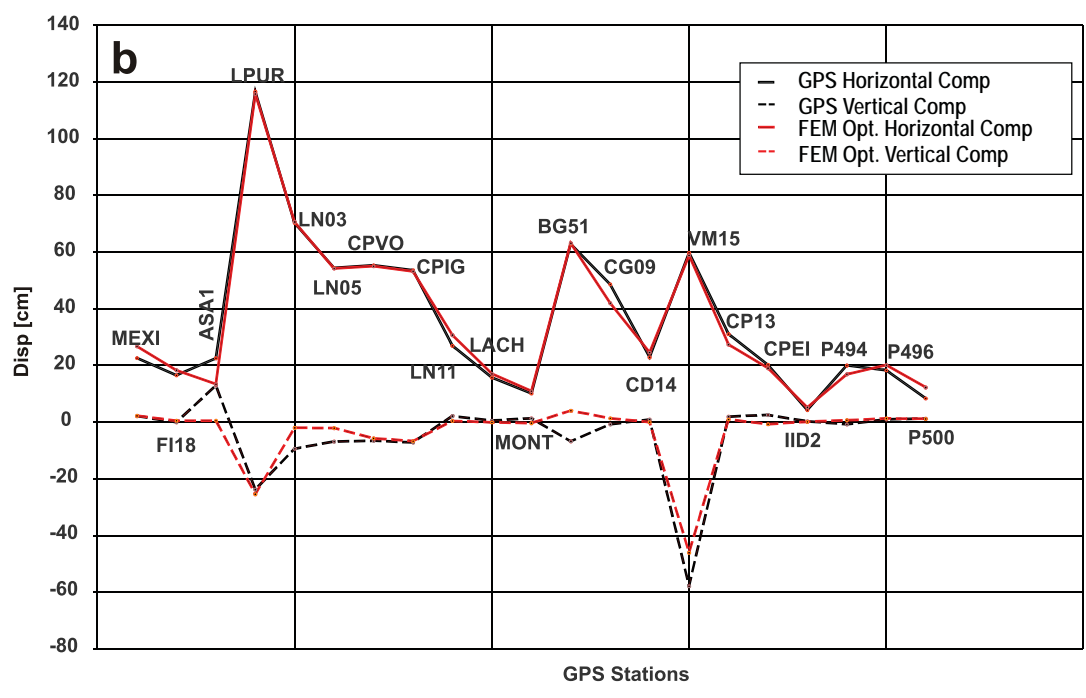
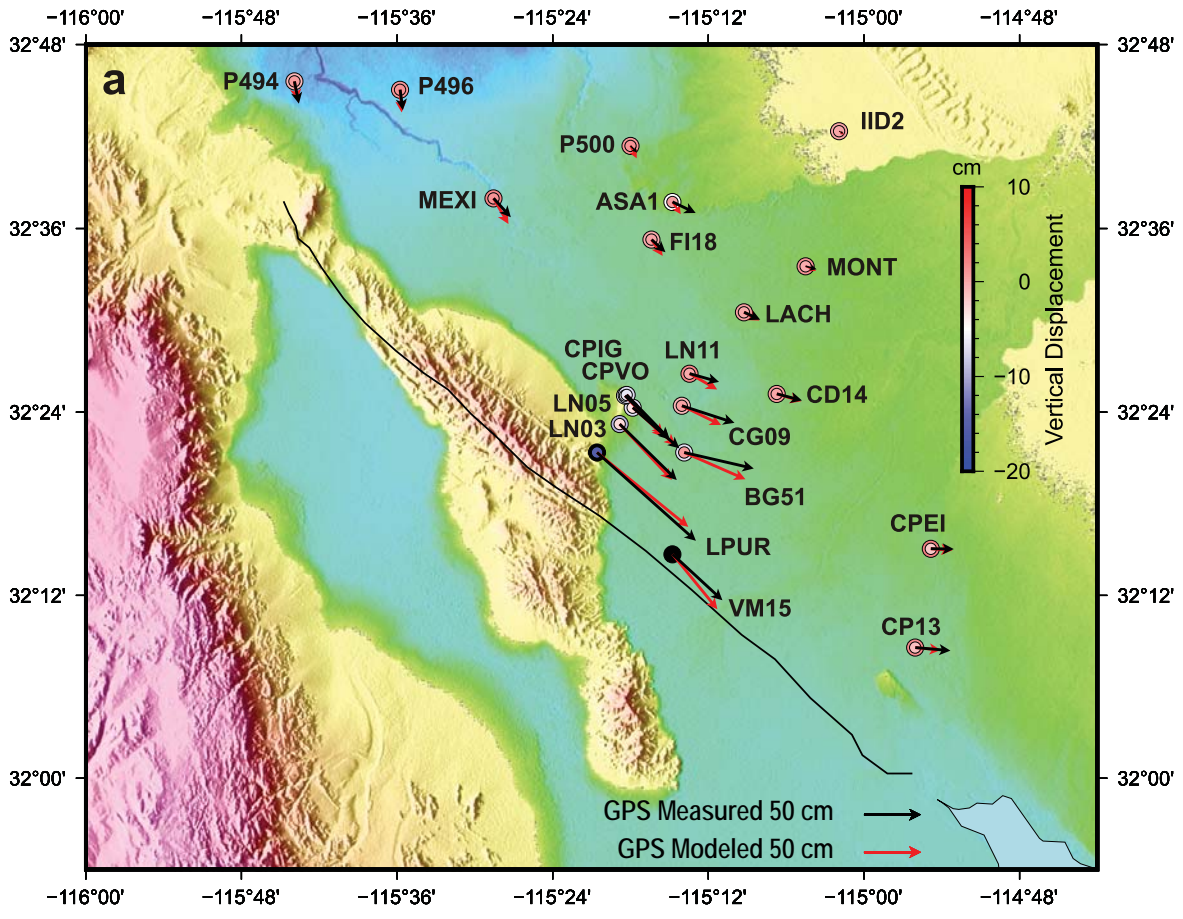


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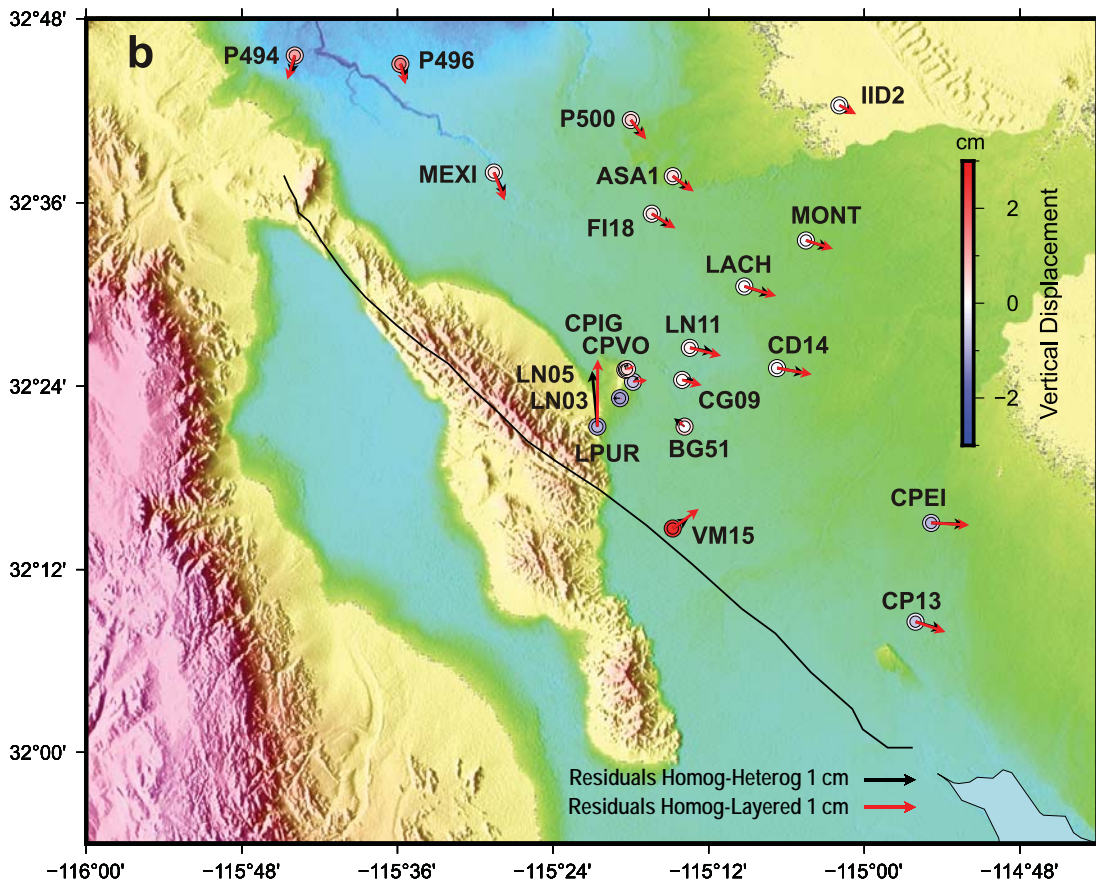
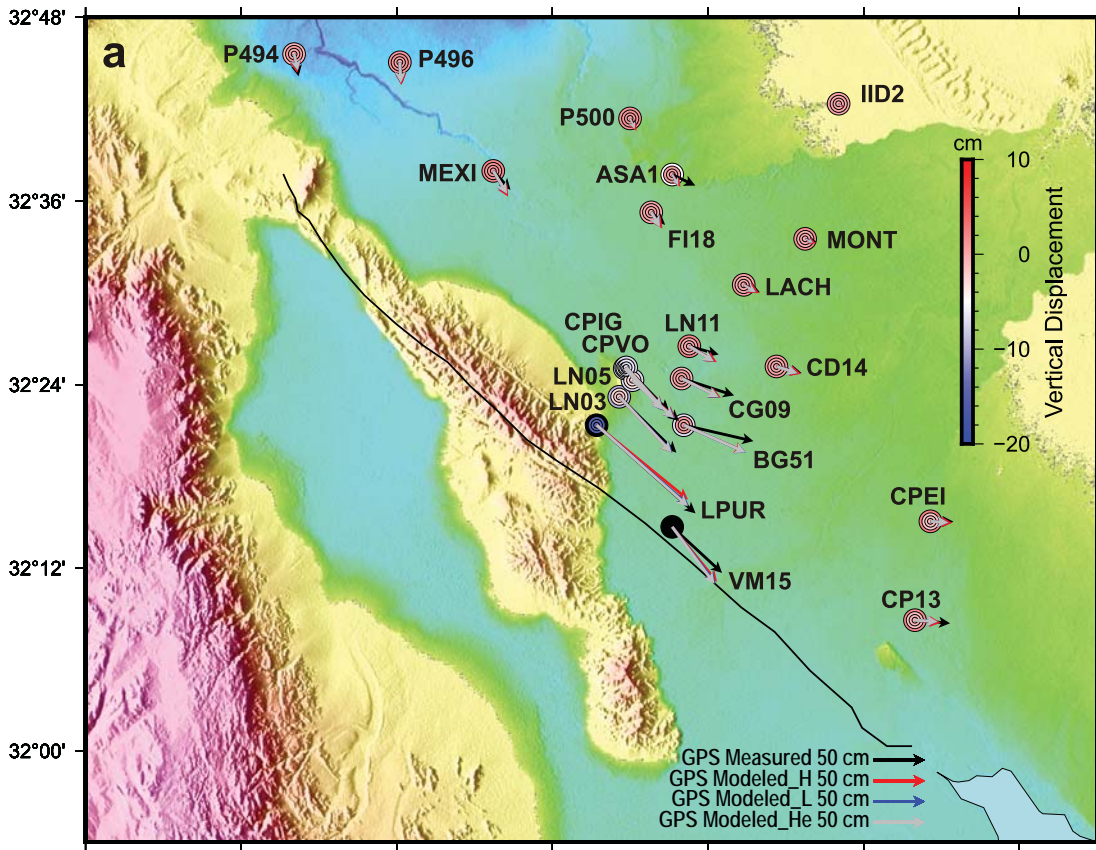


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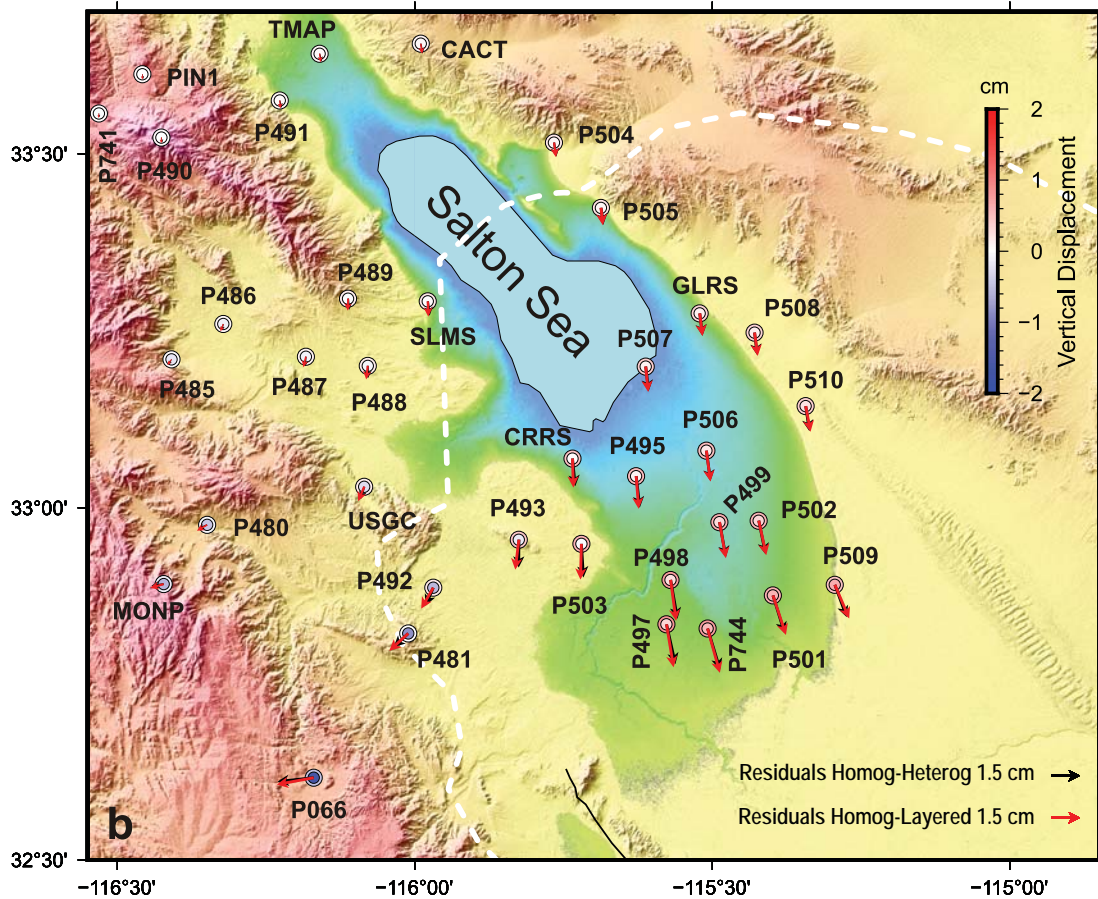
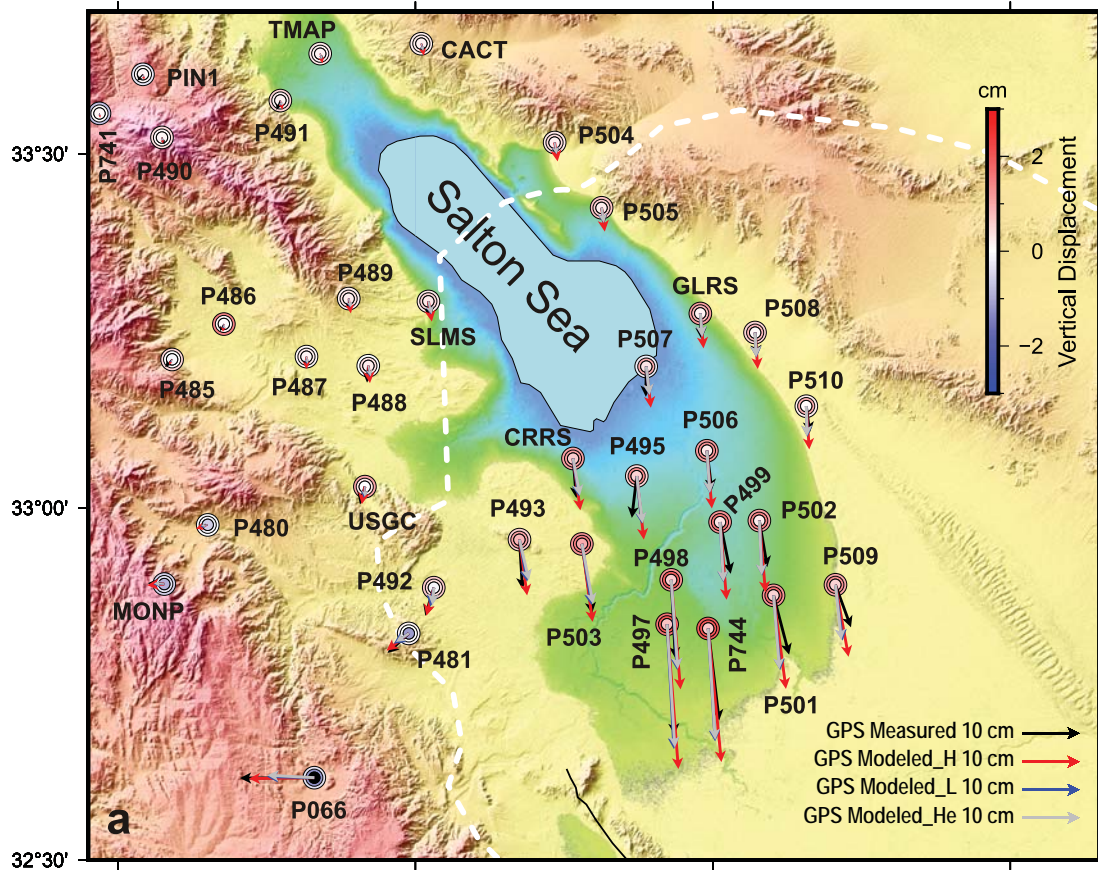


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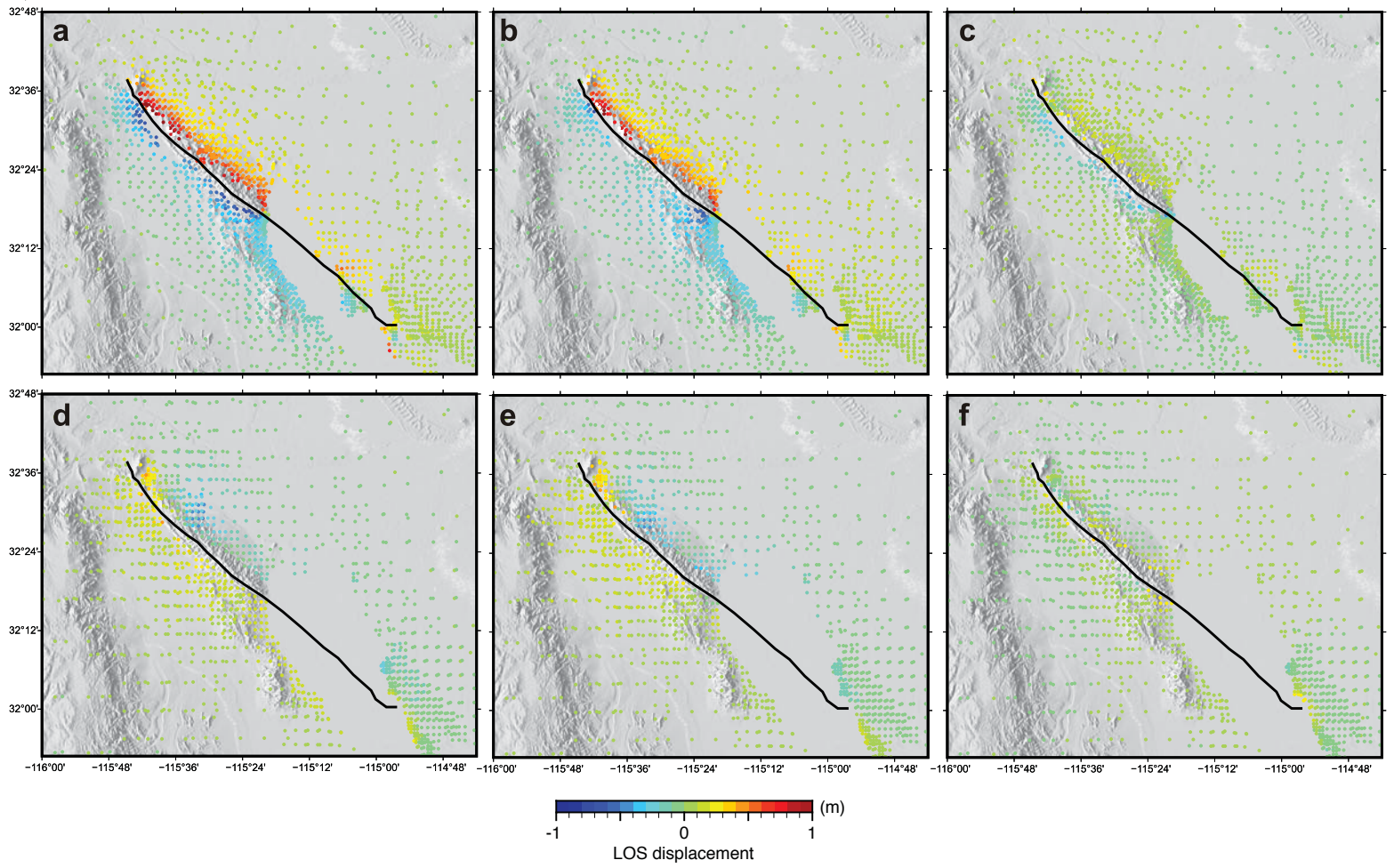


Figure 9.

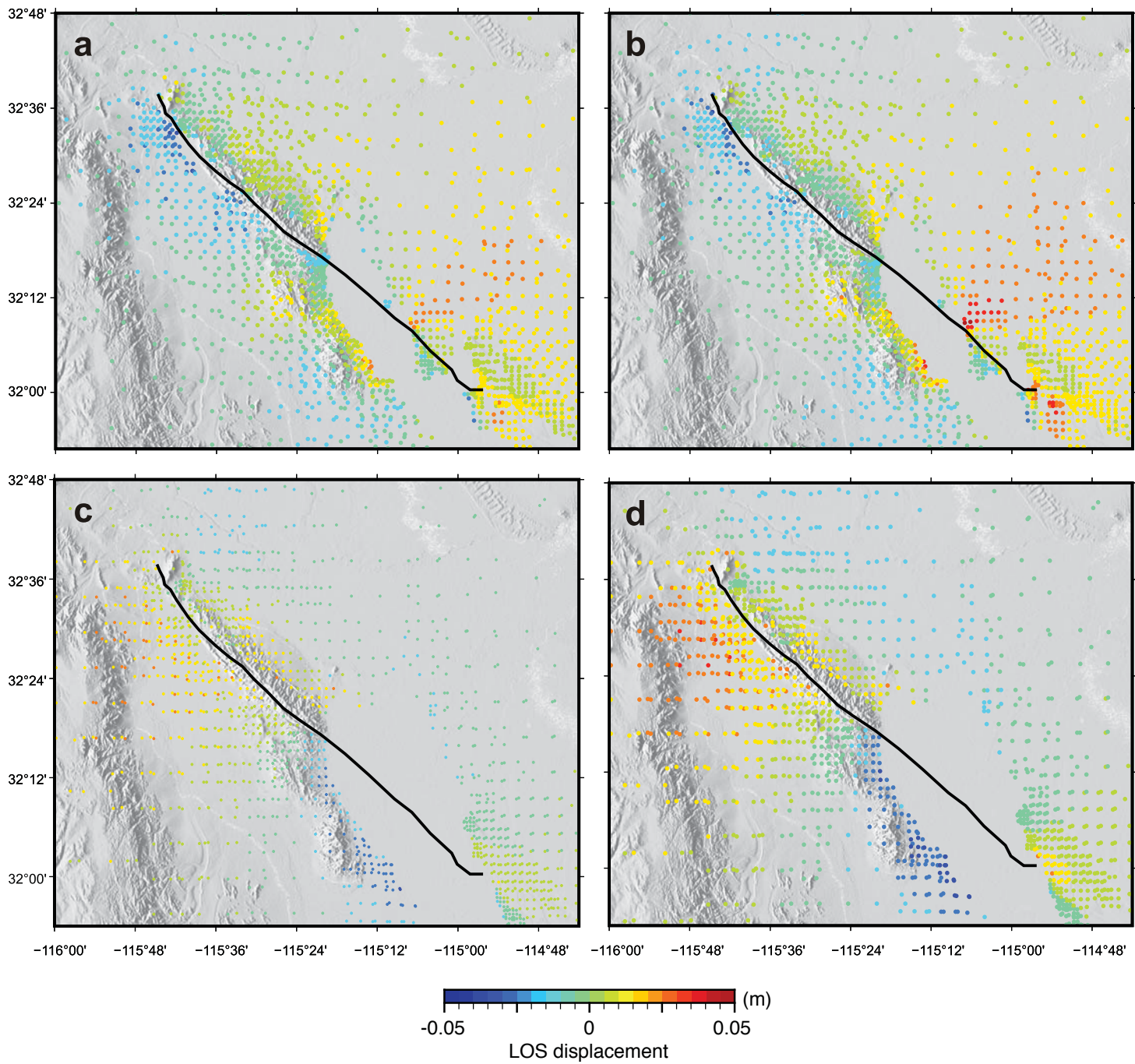


Figure 10.

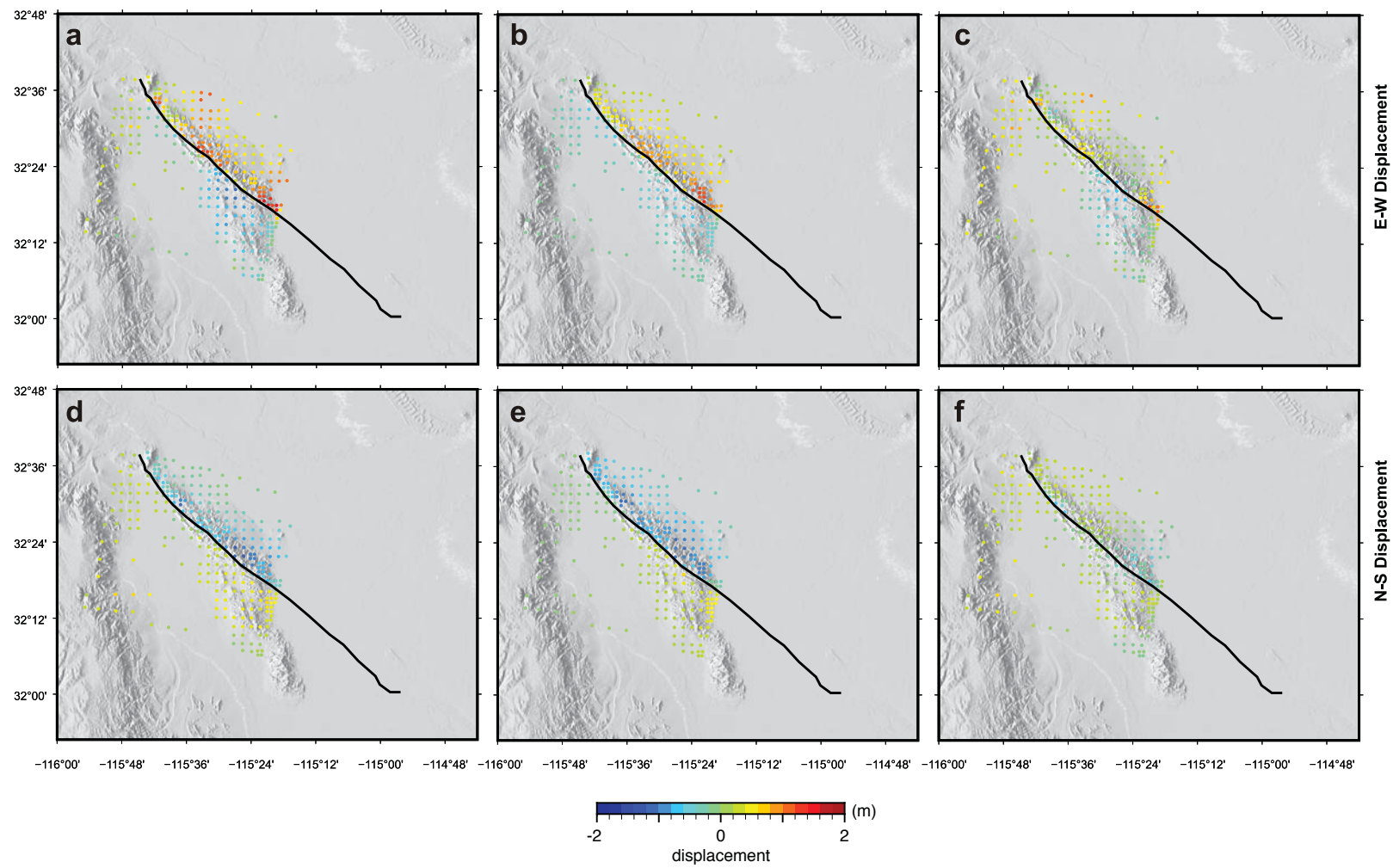


Figure 11.

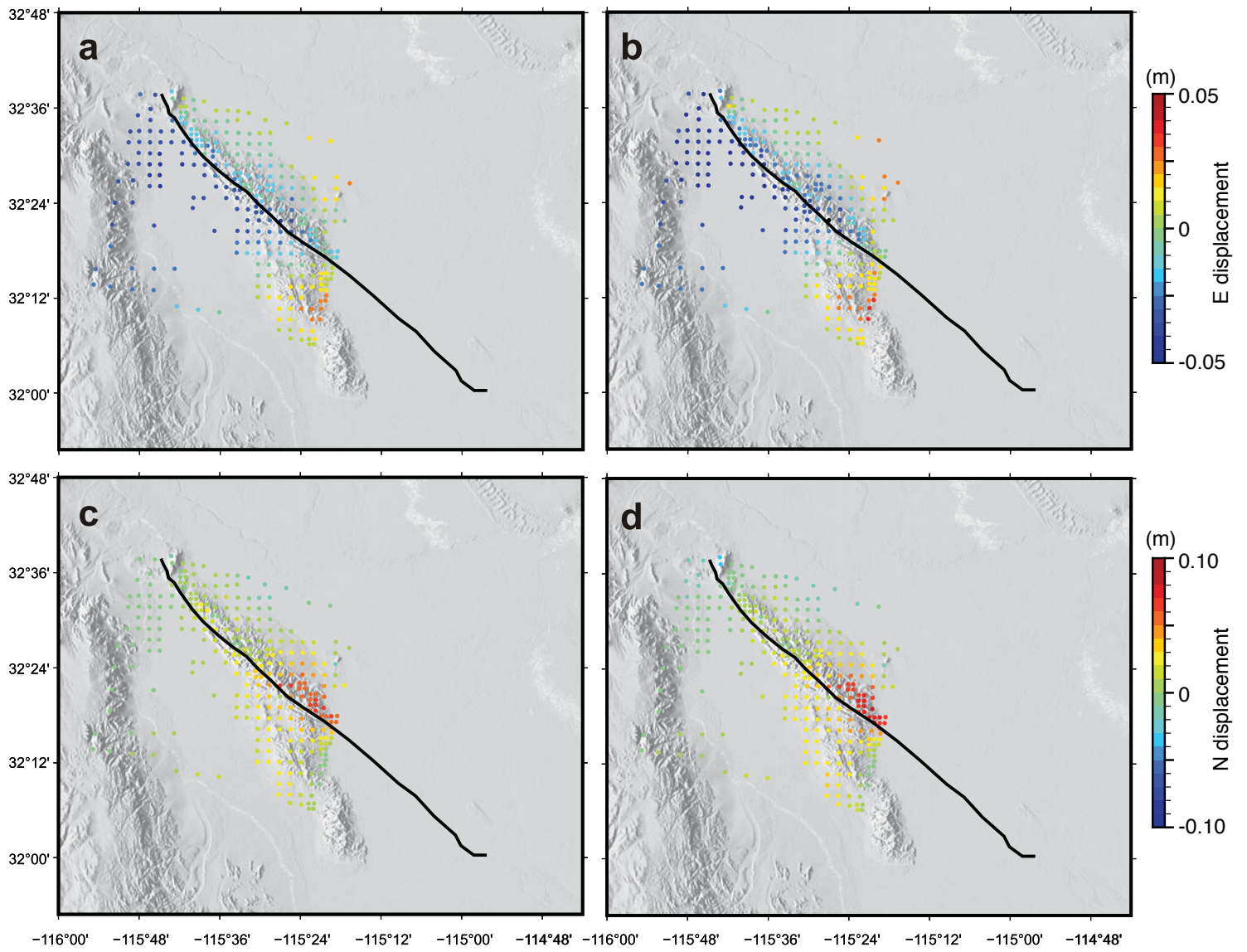


Figure 12.

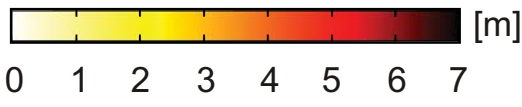
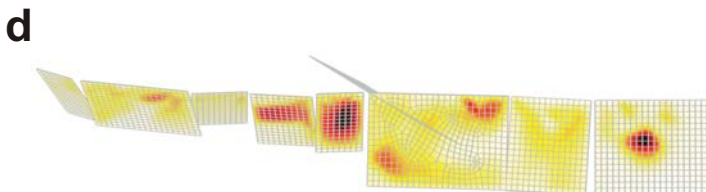
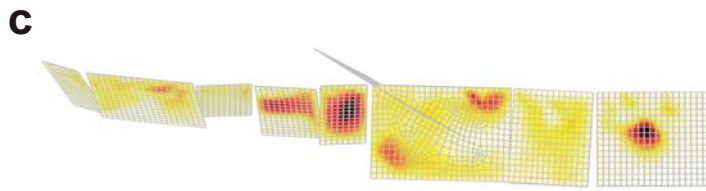
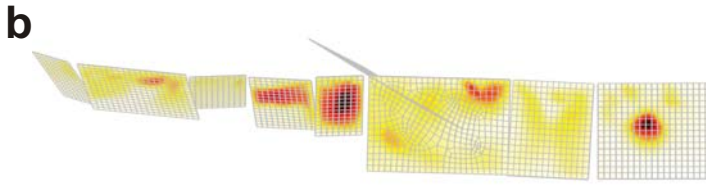
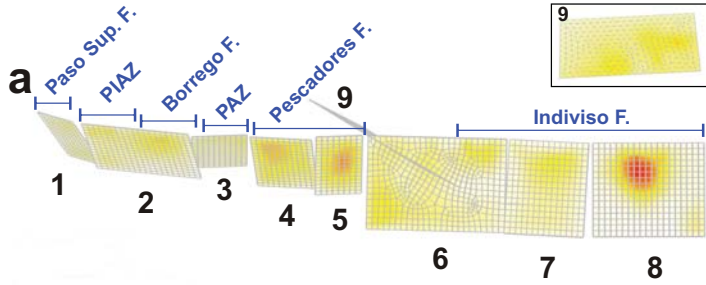


Figure 13.

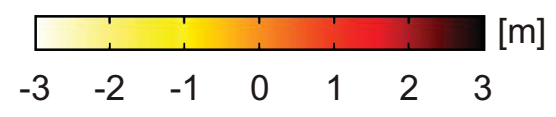
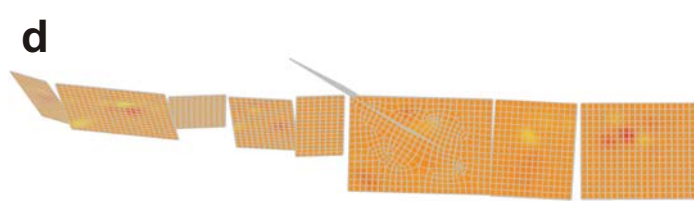
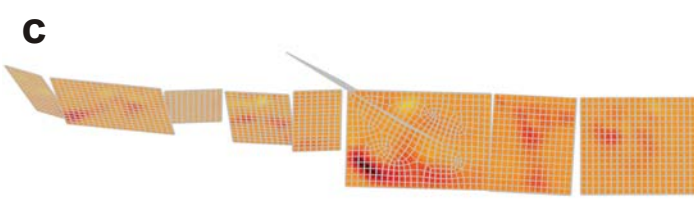
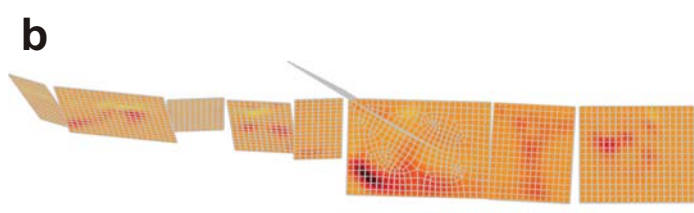
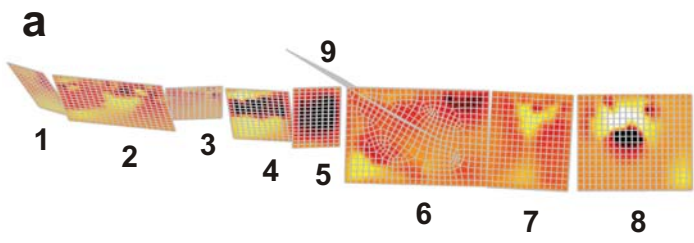


Figure 14.

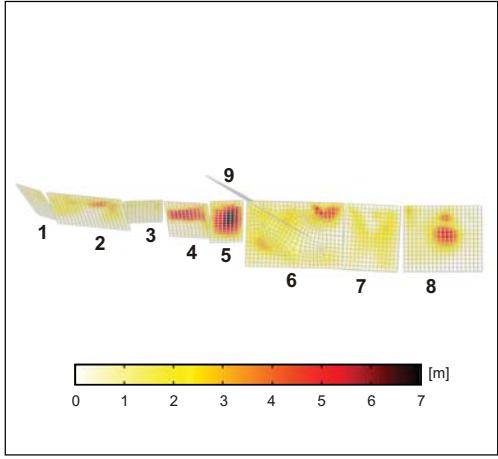


Figure 15.

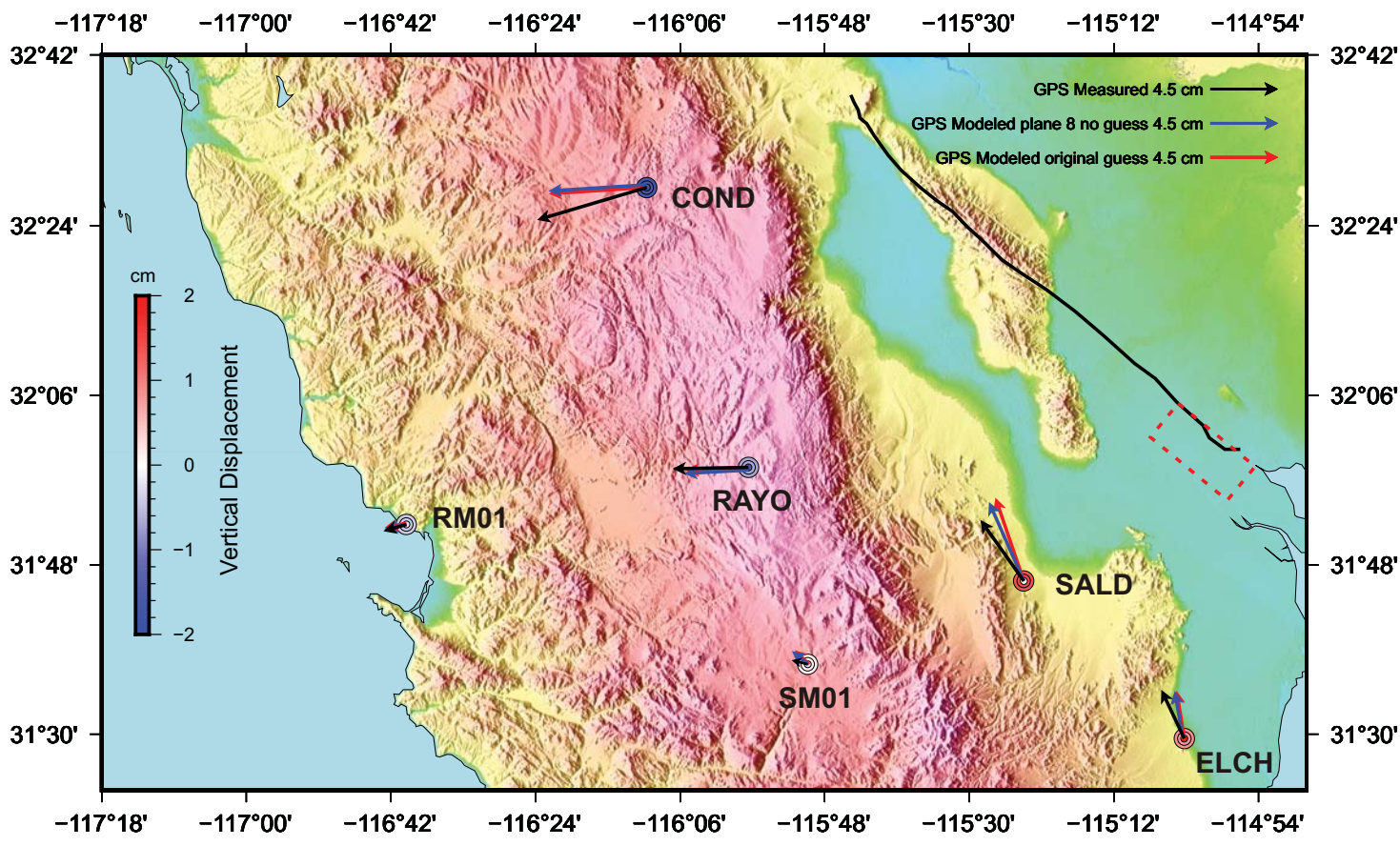


Figure 16.

